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Research paper

Geothermal modeling in complex geological systems with ComPASS

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ABSTRACT

In deep geothermal reservoirs, faults and fractures play a major role, serving as regulators of fluid flow and heat transfer while also providing feed zones for production wells. To accurately model the operation of geothermal fields, it is necessary to explicitly consider objects of varying spatial scales, from the reservoir scale itself, to that of faults and fractures, down to the scale of the injection and production wells.

Our main objective in developing the ComPASS geothermal flow simulator, was to take into account all of these geometric constraints in a flow and heat transfer numerical model using generic unstructured meshes. In its current state, the code provides a parallel implementation of a spatio-temporal discretization of the non-linear equations driving compositional multi-phase thermal flows in porous fractured media on unstructured meshes. It allows an explicit discretization of faults and fractures as 2D hybrid objects, embedded in a 3D matrix. Similarly, wells are modeled as one dimensional graphs discretized by edges of the 3D mesh which allows arbitrary multi-branch wells. The resulting approach is particularly flexible and robust in terms of modeling.

Its practical interest is demonstrated by two case studies in high-energy geothermal contexts.

1. Introduction

Geothermal resources are already widely available in areas with volcanic activity and in sedimentary basins and their exploitation could significantly contribute to the decarbonization of our economy (Hirschberg et al., 2014). In contrast to other renewable energy sources, geothermal energy is weather-independent and can provide both electricity and heat, as well as value-added mineral extraction. Geothermal power production provides reliable generation with high plant efficiency, low greenhouse gas emissions and a small ecological footprint. Moreover, it is usually a long-lasting sustainable source when properly managed (International Renewable Energy Agency and International Geothermal Association, 2023).

Numerical modeling has been one of the cornerstones of such management for decades and has become an essential tool at all stages of exploration and development of geothermal projects (O'Sullivan et al., 2001; O'Sullivan and O'Sullivan, 2016; Nugraha et al., 2022). The usual starting point is a conceptual model that often relies on 3D

geological modeling capabilities. Then, flow modeling is used during the exploration phases to understand the natural resource, to evaluate the geothermal potential, to validate conceptual hypotheses, and on the other hand, during the development of geothermal assets to predict production flow rates (e.g. among many others: Ingebritsen et al., 2010; Daniilidis et al., 2021; Jalilinasrabadly et al., 2021; O'Sullivan et al., 2009; O'Sullivan and O'Sullivan, 2016; Nugraha et al., 2022...). Not only do the models provide a coherent vision of the geothermal system by integrating all the data and measurements, but above all they represent a quantitative tool for decision making and planning production and development of the resource.

By many aspects, integrating multi-disciplinary contributions in a shared consistent numerical model of the subsurface remains a complex but worthwhile challenge to mitigate risks (Lopez et al., 2017). Passing from a 3D geological model to an hydrothermal numerical model while preserving realistic geometries in flow simulations is a crucial step of the geothermal modeling workflow (Huang et al., 2022; Nugraha

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et al., 2022). It is not so obvious to overcome. This observation was the main motivation for putting generic unstructured meshes and complex geometries at the heart of the development of the ComPASS geothermal flow simulator with the ambition to improve the accuracy and the representativeness of numerical models and simulation workflows and facilitate the back and forth between geological modeling and flow modeling.

This paper presents the ComPASS code which is an open-source, massively parallel, multi-phase, multi-component flow simulator. The paper focuses on high energy geothermal resources and how generic tetrahedral meshes can be used to exactly match any geological structure including two dimensional elements (geological interfaces, faults or fractures...) or one dimensional sharp features (surface intersections, well trajectories...). Then, adapted numerical schemes can be used in these n -dimensional elements to discretize mass and energy transfers and solve the usual, non-linear balance equations involved in geothermal reservoir modeling. In the following, we may use the term fracture for fracture or fault for brevity regardless of their geological difference.

This mixed-dimensional approach is especially useful to take into account fractures that exert a dominant control on subsurface geothermal flows and associated energy transfers. In tectonically active areas, fault zones act as permeable pathways, including high-temperature magmatic environments (Grant and Bixley, 2011; Ingebritsen et al., 2006). But this is also the case in other contexts. Concerning enhanced Geothermal Systems (EGS), where hydraulic stimulation ensures connection with a fault network, flow takes place mostly in a fracture network (Blaisonneau et al., 2021). Role of discontinuities has also been recognized as a significant factor in determining the thermal structure of sedimentary basins, as they can act as conduits linking different aquifer levels (Magri et al., 2010; Person et al., 2012; Simms and Garven, 2004). Geothermal wells are located, so that they intersect faults and fractures (Grant and Bixley, 2011). Indeed, the flow dynamics are primarily influenced by the connectivity and conductivity of the fracture network, interacting with the surrounding matrix medium.

In terms of software specifications, modeling the non-linear behavior and phase-transitions (boiling and condensation) of high-temperature geothermal brines requires quite robust algorithms. The fact that the geological media in which they flow is discontinuous because of the presence of fractures and shows abrupt petrophysical parameters variations over several orders of magnitude, with zonal anisotropies, makes accurate modeling even more challenging. For many years, Tough2 (Pruess et al., 1999; Finsterle et al., 2014) has been a de-facto industry standard (O'Sullivan and O'Sullivan, 2016) mainly thanks to its numerous and versatile *EOS modules* tailored to a large number of physics. Its large community of users contributed to this collection including for example modules for supercritical water conditions (Croucher and O'Sullivan, 2008) or brine with dissolved gas (Battistelli et al., 1997).

However, many software, including Tough2, use the classical *Two Point Flux Approximation* (TPFA) for spatially discretizing exchange terms in balance equations. TPFA relies on orthogonality conditions and limits the types of acceptable meshes, typically rectangular parallelepipedic boxes in 3D (Eymard et al., 2014). Unfortunately, using coupled finite volume schemes on such structured grids can lead to the Grid Orientation Effect (Eymard et al., 2013). Voronoidiagrams built from unstructured meshes offer more flexibility while maintaining orthogonality (Freeman et al., 2014), but they make the discretization of geological interfaces and intersections challenging, complicating the specification of domain properties and boundary conditions. All code relying on Finite Differences such as SHEMAT (Clauser, 2003) or HYDROTHERM (Hayba and Ingebritsen, 1994) suffer from these constraints as well. By design, Finite Elements based modeling suite handle nicely simplicial meshes, but tools like FEFLOW (Blöcher et al., 2010), COMSOL (Guillou-Frottier et al., 2013; Taillefer et al., 2018) or OpenGeoSys (Kolditz et al., 2012) hardly take into account phase

change with boiling or condensation and are consequently not suitable for the modeling of high temperature geothermal resources. To handle unstructured meshes, Coumou et al. (2008) implemented an operator splitting approach in the Complex System Modelling Platform (CSMP++) which involves a *thermal equilibrium* step. This approach has then been adapted to model supercritical geothermal resources (Weis et al., 2014).

Finally, it is quite common that the discretization of complex 3D geological models with unstructured good quality meshes produces hundreds of thousands to millions of cells, especially when considering regional scale models with many interfaces. In such situation, affordable computation time implies, possibly massive, parallelization of the simulation code. Among the progeny of the Tough2 family of codes, Tough3 (Jung et al., 2017) and the recent Waiwera platform (Croucher et al., 2020) offer such capabilities but suffer from the TPFA scheme limitations. CSMP++ also comes with High Performance Computing (HPC) capabilities and the DuMu^X platform is based on the modular parallel C++ framework Dune (Distributed and Unified Numerics Environment) and handle multi-phase non-isothermal flows (Koch et al., 2021).

The rest of the paper is structured in the following manner. The Section 1 presents the physical model of multi-phase compositional geothermal flows in fractured geothermal reservoirs and the specific numerical discretizations used in the ComPASS code. In addition, the approaches used in terms of meshing, parallelization and numerical performances are summarized. The Section 2 is devoted to numerical tests that demonstrate the benefits of the approach on two case studies inspired from classical high energy geothermal contexts: a liquid dominated reservoir crossed by major faults and a steam dominated reservoir.

2. Model description

In this section, we briefly review the compositional multi-phase model currently implemented in the ComPASS code as well as related numerical aspects. We refer the interested reader to already published material, especially Xing et al. (2017), Beaudé et al. (2018) and Armandine Les Landes et al. (2023), and to the publicly available [code documentation](#).

2.1. Multi-phase multi-component model

2.1.1. Physical system description

The description of the physical system is based on a Coats' type formulation (Coats, 1989) also known as *natural variables formulation*. Considering arbitrary sets of components \mathcal{C} and phases \mathcal{P} , we introduce $\mathcal{C}^\alpha \neq \emptyset$, $\mathcal{C}^\alpha \subset \mathcal{C}$ the set of components that can be present in the phase $\alpha \in \mathcal{P}$ and reciprocally $\mathcal{P}_i \neq \emptyset$, $\mathcal{P}_i \subset \mathcal{P}$ the set of phases that can contain the component $i \in \mathcal{C}$. Finally, \mathcal{Q} is a finite set of labels, called *contexts*, that are used to describe different physical states. A simple example of contexts can be $\mathcal{Q} = \{\text{liquid}, \text{gas}, \text{diphase}\}$. Building on the previous notations, each context $Q \in \mathcal{Q}$ is then associated to \mathcal{P}_Q , respectively \mathcal{C}_Q , the set of phases, respectively components, that can be present when considering context Q . It follows that $\overline{\mathcal{C}}_Q = \mathcal{C} \setminus \mathcal{C}_Q$ may be non-empty and designates the set of components that cannot be present in context Q . This framework is very generic and can be used to describe very complex fluids.

We assume thermal equilibrium between phases so that the thermodynamic characteristics of each phase $\alpha \in \mathcal{P}$ are influenced by the phase pressure P^α , the temperature T and the phase molar fractions $C^\alpha = (C_i^\alpha)_{i \in \mathcal{C}^\alpha}$. Additionally, S^α will denote the phase saturation and n_i the number of moles of component $i \in \mathcal{C}$ per unit pore volume.

Finally, the formulation uses the following set of unknowns:

$$X = ((P^\alpha)_{\alpha \in \mathcal{P}_Q}, T, (C^\alpha)_{\alpha \in \mathcal{P}_Q}, (S^\alpha)_{\alpha \in \mathcal{P}_Q}, (n_i)_{i \in \overline{\mathcal{C}}_Q}, Q). \quad (1)$$

Then, for each context Q the quantity of matter of component $i \in \mathcal{C}_Q$ writes:

$$n_i = \sum_{\alpha \in \mathcal{P}_Q \cap \mathcal{P}_i} \xi^\alpha(P^\alpha, T, C^\alpha) S^\alpha C_i^\alpha$$

with ξ^α the phase molar density, and the fluid internal energy writes:

$$E = \sum_{\alpha \in \mathcal{P}_Q} \xi^\alpha(P^\alpha, T, C^\alpha) S^\alpha e^\alpha(P^\alpha, T, C^\alpha)$$

with e^α the phase molar internal energy.

2.1.2. Fluxes and conservation laws

Molar and energy conservation provides $\#\mathcal{C} + 1$ balance equations:

$$\begin{cases} \phi \partial_t n_i + \nabla \cdot \mathbf{q}_i = 0, & i \in \mathcal{C}, \\ \phi \partial_t E + (1 - \phi) \partial_t E_r + \nabla \cdot \mathbf{q}_e = 0 \end{cases} \quad (2)$$

where ϕ is the rock porosity assumed constant in time, E_r is the fluid rock energy density. \mathbf{q}_i and \mathbf{q}_e respectively denote the molar flux of component i and the total energy flux comprising advective and diffusive transfers:

$$\mathbf{q}_i = \sum_{\alpha \in \mathcal{P}_Q \cap \mathcal{P}_i} C_i^\alpha \xi^\alpha(P^\alpha, T, C^\alpha) \mathbf{V}^\alpha,$$

$$\mathbf{q}_e = \sum_{\alpha \in \mathcal{P}_Q} h^\alpha(P^\alpha, T, C^\alpha) \xi^\alpha(P^\alpha, T, C^\alpha) \mathbf{V}^\alpha - \lambda \nabla T,$$

$$\mathbf{V}^\alpha = -\mathbf{K} \frac{k_r^\alpha(S^\alpha)}{\mu^\alpha(P^\alpha, T, C^\alpha)} (\nabla P^\alpha - \rho^\alpha(P^\alpha, T, C^\alpha) \mathbf{g})$$

which involve the generalized Darcy velocity \mathbf{V}^α , the relative permeability k_r^α , the dynamic viscosity μ^α , the mass density ρ^α , the molar enthalpy h^α of the phase α , λ the equivalent thermal conductivity of the rock/fluid mixture and \mathbf{K} the intrinsic rock permeability tensor.

To solve for the unknowns (1), the system (2) is closed by a *flash calculation* that is a fixed point equation which tracks possible context switches due to phase transitions:

$$Q = Q_{flash}(X). \quad (3)$$

and a set of local closure laws that depend on the current context:

$$\begin{cases} \sum_{\alpha \in \mathcal{P}_Q} S^\alpha = 1, \\ \sum_{i \in \mathcal{C}^\alpha} C_i^\alpha = 1, \quad \forall \alpha \in \mathcal{P}_Q, \\ P^\alpha - P^\beta = P_c^{\alpha, \beta}(X), \quad \forall (\alpha, \beta) \in \mathcal{P}_Q^2, \alpha \neq \beta, \\ f_i^\alpha(P^\alpha, T, C^\alpha) = f_i^\beta(P^\beta, T, C^\beta), \quad \forall (\alpha, \beta) \in \mathcal{P}_Q^2, \alpha \neq \beta, i \in \mathcal{C}_Q \end{cases} \quad (4)$$

where $P_c^{\alpha, \beta}(X)$ is a capillary pressure and f_i^α , the fugacity of component i in phase α , is used to write the thermodynamic equilibrium between phases.

2.2. Hybrid model with lower dimension elements

In many geothermal applications, the flow is dominated by the connectivity and conductivity of major discontinuities and feedzones are found at their intersections with wells. The main philosophy in ComPASS is to rely on the versatility of unstructured meshes to exactly match any geological structure and two dimensional geometrical objects and boundaries (geological interfaces, fractures...) or one dimensional sharp features (surface intersections, well trajectories...). Depending on the geological model, producing this kind of conformal meshes with relatively good quality elements can be challenging and it is a crucial step in the whole workflow (Balarac et al., 2022). An alternative, would be to model lower dimensional entities as with distinct meshes and consider them as *embedded features* which then adds a complexity in terms of coupling (Cusini et al., 2021).

2.2.1. Discrete fractures

ComPASS implements a Discrete Fracture Matrix (DFM) method, where fractures are discretized by a subset of the 3D mesh facets which incorporate a lower-dimensional physical model. The latest is created by averaging the Eqs. (2), as well as the unknowns (1) related to fractures across their respective widths (Xing et al., 2017).

The transmission conditions that exist at the interfaces between the matrix and fractures depend on extra physical assumptions regarding their drain or barrier behavior of fractures. When they are conductive in terms of both permeability and thermal conductivity, pressure and temperature continuity can be assumed as matrix fracture transmission conditions in single-phase flows (Serres et al., 2002; Brenner et al., 2016). This approach has been expanded to encompass two-phase Darcy flows (Bogdanov et al., 2003; Reichenberger et al., 2006; Brenner et al., 2015, 2017) as well as multi-phase compositional thermal Darcy flows (Xing et al., 2017).

2.2.2. Multi-branch well model

One of the main challenges in well modeling in field simulation is the significant difference between the kilometer scale reservoir and the decimeter scale radius of the wellbore. The well geometry cannot be resolved explicitly by the mesh, so the well is modeled as a line source defined by a one-dimensional graph with a rooted tree structure. This graph can accurately depict sloped and multi-branch wells, and it is discretized by a subset of edges on which the mesh is based.

The flow within the well is locally connected to both the 3D matrix surrounding the well and the fractures that intersect the well. The mass and heat exchanges for each node of the well in contact with a fracture or the rock mass are modeled using the Peaceman approach (Peaceman, 1978, 1983). This approach is widely used in reservoir simulation and involves discretizing the Darcy or Fourier fluxes between the reservoir and the well using a two-point flux approximation. The transmissivity takes into account the unresolved pressure or temperature singularity within the well. At the discrete level, the well index or Peaceman's index depends on the type of cell, well radius and geometry, and the discretization scheme used (Wolfsteiner et al., 2003; Aavatsmark and Klausen, 2003; Chen and Zhang, 2009; Yapparova et al., 2022).

In the present work, we use an extension of the simple well model detailed by Beaudé et al. (2018) to two-phase flows. The wellbore flow is assumed stationary and by explicitly calculating the pressure drop, the well model is simplified to a single equation with a single implicit unknown which represents the reference pressure of the well. Pressures and saturations along the well are then deduced from this reference pressure and the explicit expression of pressure losses taking into account gravity. To monitor the well, complementary conditions are prescribed between the mass flow rate and the wellhead pressure. For production (resp. injection) wells, they are based on a maximum (resp. minimum) mass flow rate and a minimum (resp. maximum) wellhead pressure. Though a single unknown is introduced, all nodes along the well path are linked to the well reference pressure and this results in additional connectivity in the system, which needs to be taken into account when parallelizing the code (Beaudé et al., 2018).

2.3. Spatial discretization

The discretization of the spatial terms involved in the continuous model introduced previously relies on the Vertex Approximation Gradient (VAG) finite volume scheme (Eymard et al., 2012). This scheme belongs to the family of gradient schemes (Droniou et al., 2010) and is particularly adapted to the resolution of Darcy's law on conformal polyhedral meshes. The VAG discretization has been adapted to mixed-dimensional modeling (Brenner et al., 2016, 2015). Two-phase Darcy flows discretization was introduced by Brenner et al. (2015) and generalized to multi-phase multi-component flows by Xing et al. (2017). We approximate Darcy fluxes mobilities using a phase potential upwind scheme.

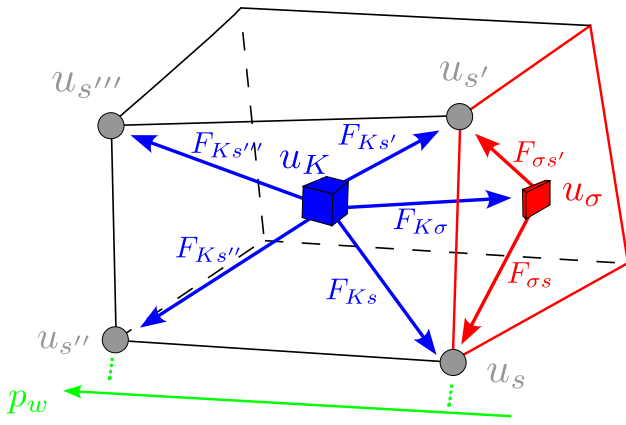


Fig. 1. For a cell K and a fracture face σ (in bold), examples of VAG degrees of freedom $u_K, u_s, u_{s'}, u_{s''}$ and VAG fluxes $F_{K,\sigma}, F_{K,s}, F_{K,s'}, F_{\sigma,s}$.

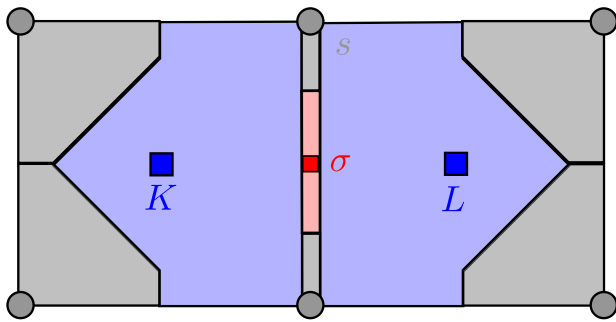


Fig. 2. Example of control volumes at cells, fracture face, and nodes, in the case of two cells K and L split by one fracture face σ (the width of the fracture is enlarged in this figure). The control volumes are chosen to avoid mixing fracture and matrix rocktypes.

Fig. 1 details the different degrees of freedom introduced by the VAG scheme and their associated fluxes. It shows one polyhedral cell K (blue) with one fracture face σ (red). The 3D matrix fluxes (blue arrows) connect K to cell nodes (e.g. s, s', s'', s''') and fracture faces when present (e.g. σ). The 2D fracture fluxes (red arrows) connect each fracture face σ to its nodes (e.g. s, s'). Finally, nodes that are on a well path (e.g. s, s'') are also involved in two-point fluxes with the well bore flow (green arrow).

Then, the volume of each cell is partitioned so that a control volume is associated with each degree of freedom. Compared to other approaches like Control Volume Finite Element Methods (CVFE), the VAG scheme's crucial advantage is the flexibility it offers in selecting the control volumes. We exploit it to ensure that there is no mixing of heterogeneous properties within each control volume nor between matrix and fracture media (Fig. 2) which limits numerical diffusion.

2.4. Numerical aspects

2.4.1. Non-linear solver

A fully implicit Euler scheme is then used to integrate the semi-discrete problem obtained in Section 2.3 and results in a non-linear problem with unknowns consisting in reservoir unknowns (1) and a reference pressure for each of the wells. Because of the flash fixed point equations (Eq. (3)) at each degree of freedom, the problem is solved using an active set Newton–Raphson algorithm (Coats, 1989).

As VAG matrix fluxes are expressed linearly and locally to each cell (Fig. 1), the rows of the Jacobian matrix involved in each Newton iteration and corresponding to the balance equations of the control volumes associated with cells can be eliminated without any fill-in.

Thanks to this elimination, and the use of vertices as main degrees of freedom during the resolution step, the VAG scheme maintains a comparable cost to nodal methods on unstructured meshes though it introduces many degrees of freedom (Brenner et al., 2015). It is particularly suitable to work with tetrahedral meshes that have much more cells than vertices.

The size of the Jacobian matrix is also controlled using the discrete version of the local closure Eqs. (4) to divide the reservoir unknowns into primary and secondary unknowns. The latter are expressed locally as a function of the former and eliminated from the Jacobian matrix.

An iterative solver, typically GMRES, is used to solve the resulting ill-conditioned linear system. A preconditioner is applied to the solver, which is adapted to the pressure unknown's elliptic or parabolic nature and to the coupling with the remaining hyperbolic or parabolic unknowns. The CPR-AMG preconditioner is considered to be one of the most efficient preconditioners for such systems (Lacroix et al., 2001; Scheichl et al., 2003). We refer to Xing et al. (2017) and Beaudé et al. (2018) for the full details of its implementation.

2.4.2. Parallel implementation

The assembly and resolution of linear systems, which are involved in solving the fully coupled non-linear problem, are performed in parallel using the Single Program Multiple Data (SPMD) paradigm. The rows of the global system are distributed in a well balanced manner to available processes (Xing et al., 2017). To be able to assemble these rows, degrees of freedom holding system unknowns (nodes s , fracture faces σ , cells K and wells w) must also be distributed between processes, minimizing the need for communications.

At the beginning of the simulation, the mesh's cells set is partitioned using the METIS library (Karypis and Kumar, 1998) and each resulting subdomain is linked to a unique process rank. Then, node and fracture degrees of freedom are distributed to processes according to the cells they are connected to. Elements belonging to the interior of a cell subdomain are unambiguously attributed to the associated process whereas an arbitrary but reproducible choice is made for boundary elements (Xing et al., 2017).

Ghost elements are added to each subdomain to synchronize unknowns between adjacent degrees of freedom. At the subdomain boundaries, a single layer of ghost cells is added, along with all the intersecting nodes and fracture elements (Xing et al., 2017). Concerning wells, reference pressure unknowns are associated to a mesh vertex (node) and are innately associated with the same process rank as this vertex. However, all nodes that belong to a well path are created and synchronized across each subdomain that intersects the well path. This approach enables the local re-computation of well states on any subdomain affected by well operations without requiring communication between processes (Beaudé et al., 2018).

Once this distribution is made, meshes are locally reconstructed. At each Newton–Raphson iteration, a linear system that corresponds to the rows of the system is created locally on each process using both its own and ghost (i.e. synchronized) unknowns. Once assembled, the system is transferred to the PETSc parallel linear solver library (Balay et al., 2014). The parallel matrix and vector are stored in PETSc such that each process stores its own rows, which perfectly fits our design. The GMRES/CPR-AMG combination outlined previously is implemented using PETSc Krylov subspace iterative method framework. Following resolution, the ghost unknowns are retrieved through a synchronization step using restriction matrices and PETSc matrix–vector product.

Scalability tests can be found in Xing et al. (2017) and Armandine Les Landes et al. (2023) and show good behavior of the ComPASS code with the usual observation that the strong scalability is limited by the AMG-type preconditioner and requires a sufficiently high number of unknowns per processor (of the order of 10^4 pressure unknowns per processor).

In addition to enhancing computational efficiency, these technical aspects facilitates the development of high-resolution geological models

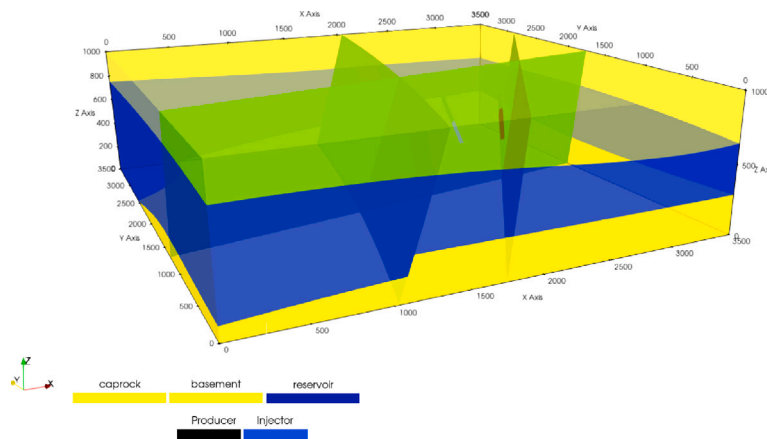


Fig. 3. Geometry and mesh of the domain modeled.

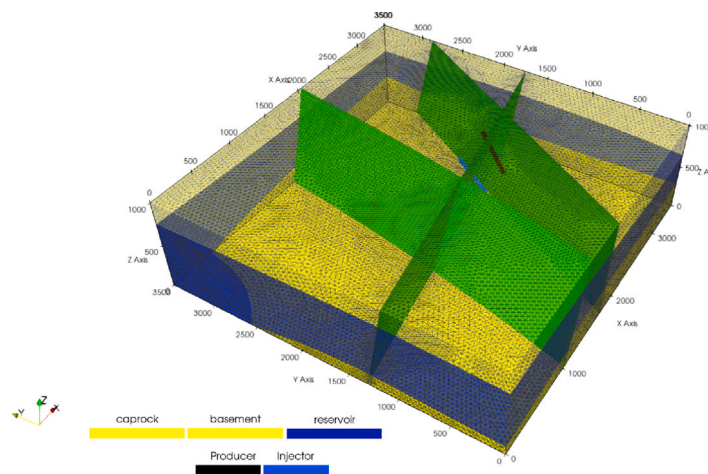


Fig. 4. Mesh and wells location.

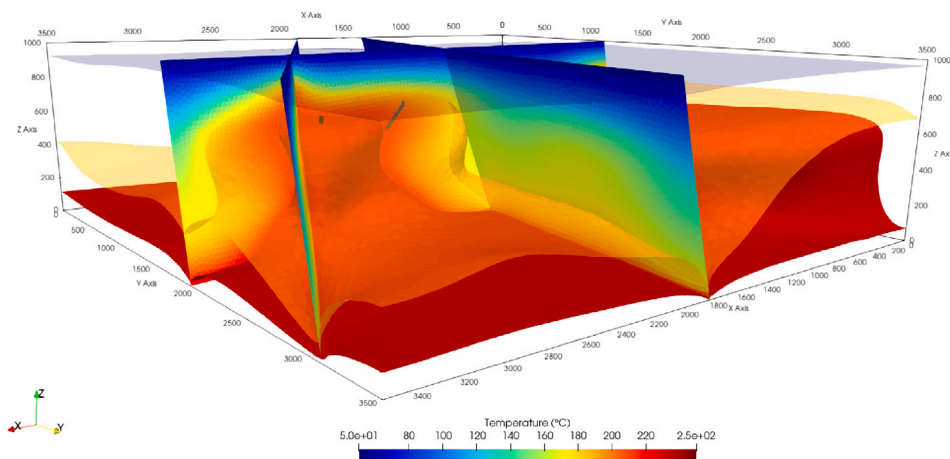


Fig. 5. Isotherm surfaces of 50 °C, 190 °C and 250 °C at the initial state, dominated by convection.

as well as larger-scale simulations. These models not only deepen our understanding of subsurface processes but also serve as valuable tools for environmentally sustainable geoscientific exploration and project management. Furthermore, they provide the computational infrastructure necessary for incorporating advanced algorithms, integrating interdisciplinary research with machine learning and artificial intelligence into resource assessment and management practices (Achyut and

Haese, 2023; Wycisk et al., 2009; Meckel and Beckham, 2022; Zayed et al., 2023; Żuk, 2024).

2.4.3. Application programming interface

Whereas previous versions of COMPASS were implemented in pure Fortran, COMPASS 4 introduced a breaking change with the ability to set-up a simulation and control most of the timeloop execution using

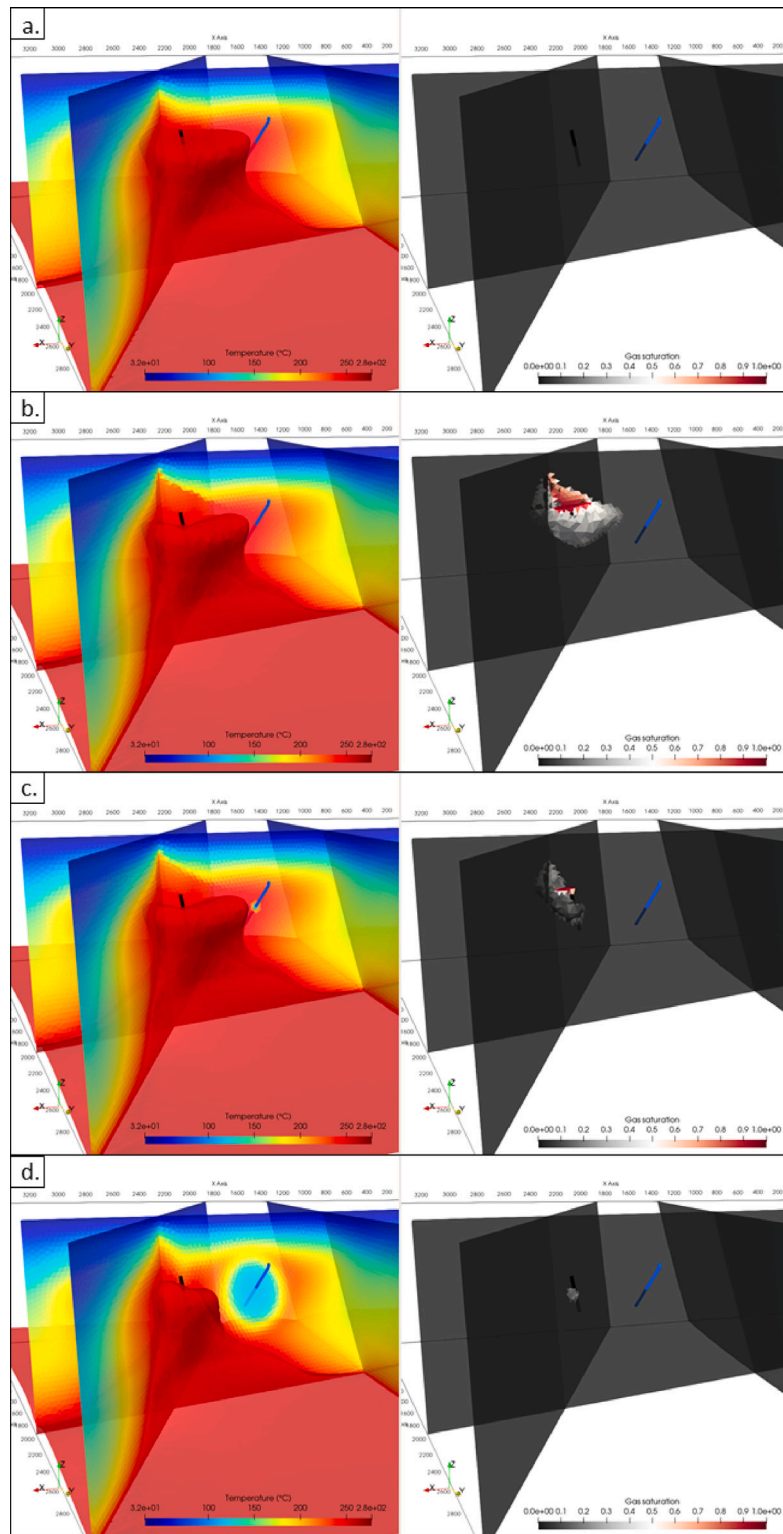


Fig. 6. Left: Temperature evolution (°C) at multiple times within the faults and within the domain (isotherm surface of 250 °C). Right: Gas saturation evolution (isosaturation surface of 0.1) at multiple times: 0, 2, 3.1 and 20 years.

the high level Python language. The Python layer is not a mere set of routine to pre- or post process data but rather a full Application Programming Interface (API) with the long term ambition to provide a full numerical development environment for reservoir engineers and numerical expert.

Building on the simplicity and efficiency of the Python language, one can set-up complex simulations or quickly adapt example scripts

or explore simulation results. Some of the physical laws, such as relative permeabilities, capillary pressures, can also be specified by the user directly in Python without the need for compilation, either using an explicit formula or choosing one of the available models. The seasoned user can also build complex physical and/or numerical experiments (Amir and Kern, 2021) without the burden of recompiling the software and without loss of performance.

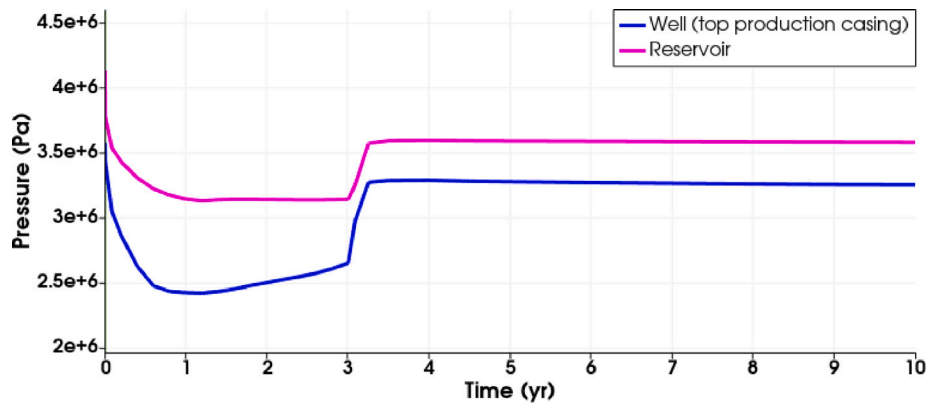


Fig. 7. Pressure at the top depth in the producer well and in the reservoir as function of time.

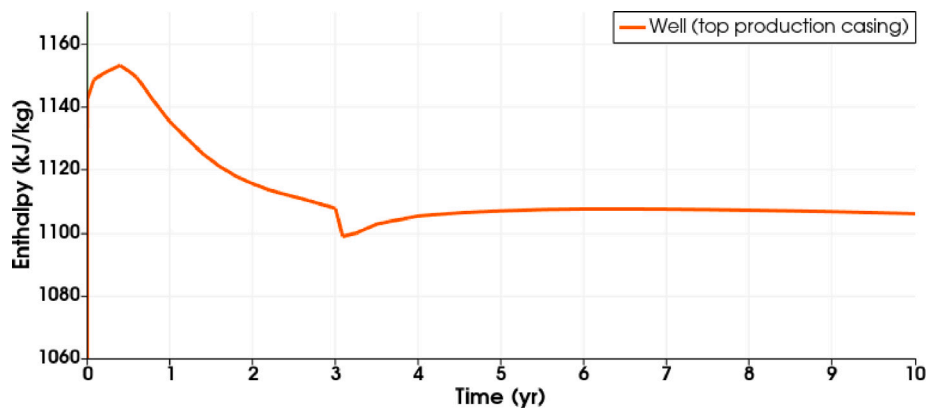


Fig. 8. Energy flow rate at the top depth in the producer well and in the reservoir as function of time.

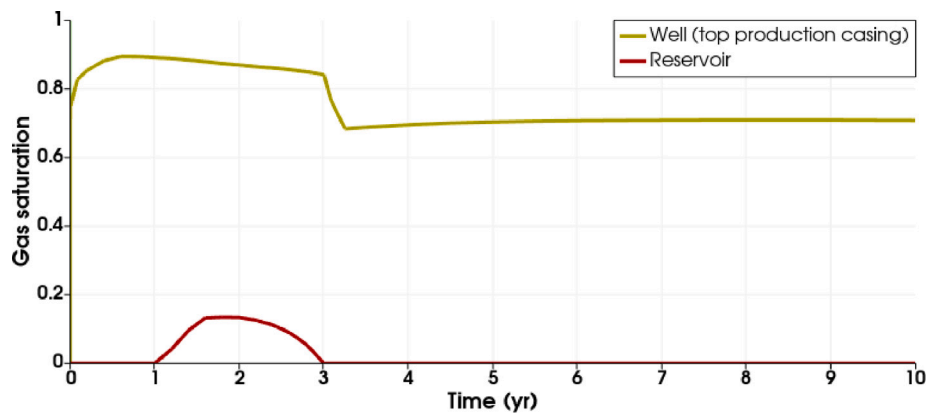


Fig. 9. Gas saturation at the top depth in the producer well and in the reservoir as function of time.

Currently, the simulation outputs are saved as compressed binary NumPy arrays and post-processing routines are provided to convert them to *Paraview* parallel file formats.

2.4.4. Meshing

Though meshing techniques are not the central part of our work, exploiting the full potentialities of the ComPASS code assumes that one is able to generate good-quality conformal meshes out of complex geological models. A conformal mesh is a mesh such that intersection of any two distinct elements (vertices, edges, faces or cells) is either void either one, and only one, of these elements. Moreover, there are several quality criteria concerning the mesh whose general idea is that the spatial elements are well proportioned not being too flat or distorted.

Such ill proportioned elements are well known to create numerical difficulties in reservoir simulation. Though the VAG scheme performs noticeably well on such meshes (Eymard et al., 2011), a good quality mesh will always make the simulation easier, especially when dealing with multi-phase simulations.

In the following section, we used *Salome platform* to generate conformal meshes that represent complex geological models. The approach is explicit in the sense that surfaces have been constructed first to represent either faults or layer boundaries. The surfaces composing such a B-Rep (Boundary Representation) model are then meshed with triangles. In a last step the meshing algorithm generates a tetrahedral discretization of the connected components between surface boundaries (Ribes and Caremoli, 2007; Schöberl, 1997). Each of the elements

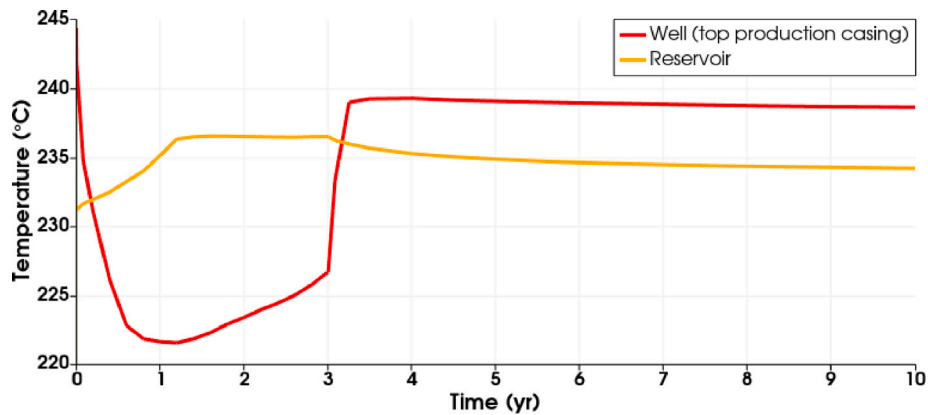


Fig. 10. Temperature at the top depth in the producer well and in the reservoir as function of time.

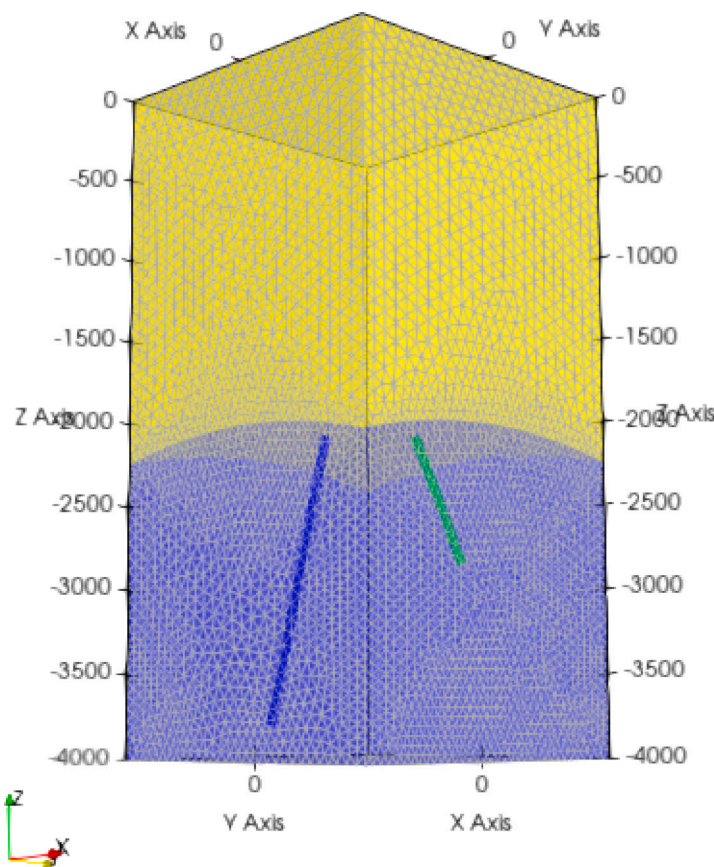


Fig. 11. Domain modeled with the reservoir (in blue) and the caprock (in yellow), the mesh and the wells location : injector (in blue) and producer (in green).

of interest (geological surfaces, fractures, well paths...) are tagged with specific codes using the Salome interface. The codes are then retrieved in the ComPASS simulation using an ad-hoc reader that was developed on purpose and can be used to assign different physical properties. This reader can be easily adapted to any meshing framework.

3. Case studies

ComPASS continuous integration tests include simple synthetic test cases and additional baseline test cases taken from geothermal code

comparison projects (Molloy and Sorey, 1981). These may serve as tutorials and/or template for new simulations.

The next sections focus on two imaginary field studies and highlight the advantages of the ComPASS platform to describe complex geological settings and various physical conditions of high-energy geothermal resources: a liquid dominated reservoir crossed by major faults, inspired from the Bouillante geothermal field (Guadeloupe, West Indies) and a low pressure steam dominated reservoir inspired from the Larderello field (Italy). In both case studies a subcritical single-component (water) two-phase model is employed with three contexts ($\mathcal{Q} = \{gas, liquid, diphasic\}$).

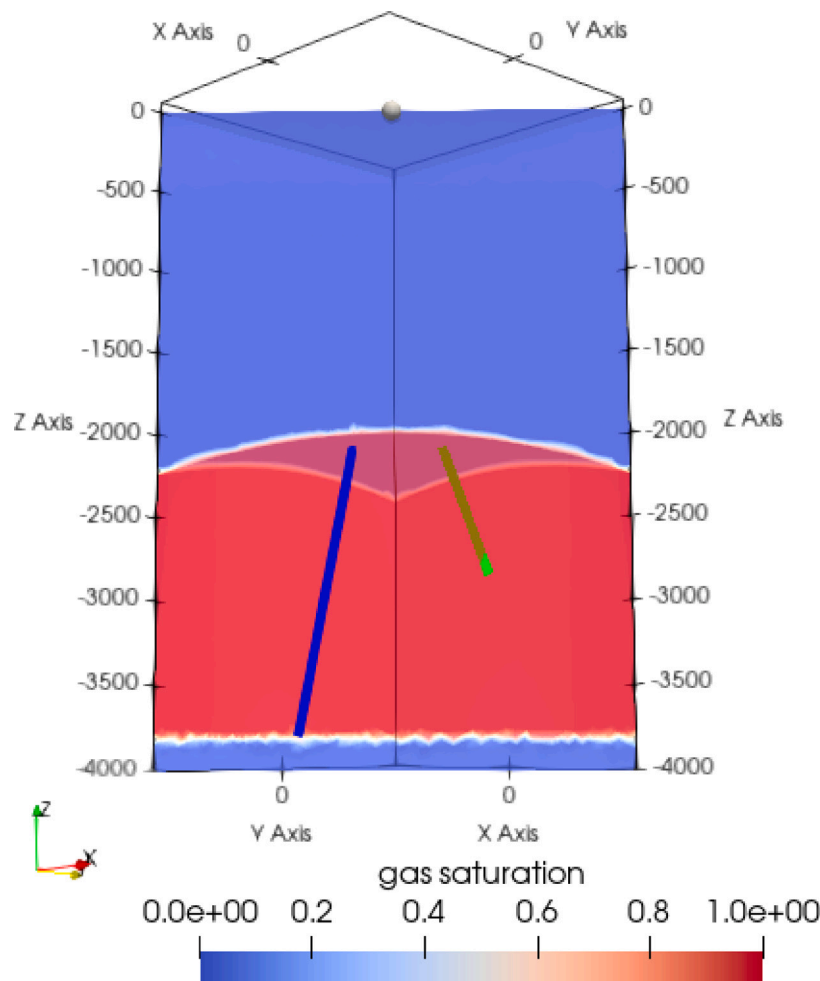


Fig. 12. Gas saturation at the initial state of the steam-dominated reservoir.

3.1. Liquid dominated reservoir

3.1.1. Context, objective and geometry

We consider a 500 m thick liquid-dominated geothermal reservoir, in a volcanic (blue domain in Fig. 3) intersected by several sub-vertical faults. The reservoir is overlaid by a weakly permeable altered caprock (top yellow domain in Fig. 3) with a 250 m thickness. The basement layer (bottom yellow domain in Fig. 3), underlies the reservoir.

The conformal tetrahedral mesh is made of more than 100,000 nodes and nearly 600,000 cells. Fig. 4 shows 2D elements (geological horizons and fault surfaces), respectively 1D elements (well paths), discretized by triangle facets, respectively edges.

The geothermal field is operated using a doublet of two deviated wells: a producer (black line in Fig. 4) and an injector (blue line in Fig. 4). Both wells are open hole in the whole reservoir and intersect the same major fault at approximately 400 m below surface.

3.1.2. Hydraulic and thermal properties

The caprock and basement layers have low homogeneous and isotropic permeability of 10^{-18} m^2 . The reservoir is assumed homogeneous and has a 10^{-14} m^2 isotropic permeability and 0.05 porosity. Faults are described by a 10 m thick damaged area, a 5.10^{-14} m^2 permeability and a 0.2 porosity. Upper portions of the faults, that lie in the alteration zone of the caprock, are treated as having low permeability. The rock thermal properties and density are homogeneous for the whole rock mass with thermal conductivity $\lambda = 3 \text{ W K}^{-1} \text{ m}^{-1}$, specific heat capacity $c_p = 1000 \text{ J kg}^{-1} \text{ K}^{-1}$, and density $\rho_{rock} = 2600 \text{ kg m}^{-3}$.

3.1.3. Initial and boundary conditions

Natural state of the geothermal system, is achieved by performing a simulation over a long period of 10^5 years. The simulation begins with a hydrostatic pressure state of 1 bar at the top of the model, and the temperature field gradually increasing linearly with depth, ranging from $30 \text{ }^\circ\text{C}$ at the top to approximately $280 \text{ }^\circ\text{C}$ at the bottom, until a steady-state is reached. Temperature and pressure are assigned Dirichlet boundary conditions at the top and bottom boundaries, while no-flow boundary conditions are imposed on all four lateral boundaries.

After 10^5 years, the geothermal system reaches a stable convective state: the temperature field displays the formation of convection cells, controlled by the highly permeable faults acting as drains. Iso-temperature surfaces of $190 \text{ }^\circ\text{C}$ and $250 \text{ }^\circ\text{C}$ highlight this phenomenon (Fig. 5).

In this natural state, the geothermal fluid remains liquid throughout the entire domain. The producer well (black line in Fig. 6) is located close to the intersection of two faults, in order to exploit the warmest (and shallowest) region located at the apex of an upflowing plume. In this region, the temperature reaches approximately $250 \text{ }^\circ\text{C}$ (Fig. 6.a).

3.1.4. Exploitation scenario

The operating conditions simulation are as follows. The reservoir is first produced with a constant flow rate of 180 ton h^{-1} for a period of three years without reinjection. Then, reinjection begins, with 80% of the produced fluid being injected back into the reservoir via the injection well, with a wellhead temperature of $110 \text{ }^\circ\text{C}$. Dirichlet boundary conditions corresponding to natural state are enforced at the top and bottom boundaries of the domain. Consequently, the reservoir is not entirely isolated and is partly recharged through the fault network.

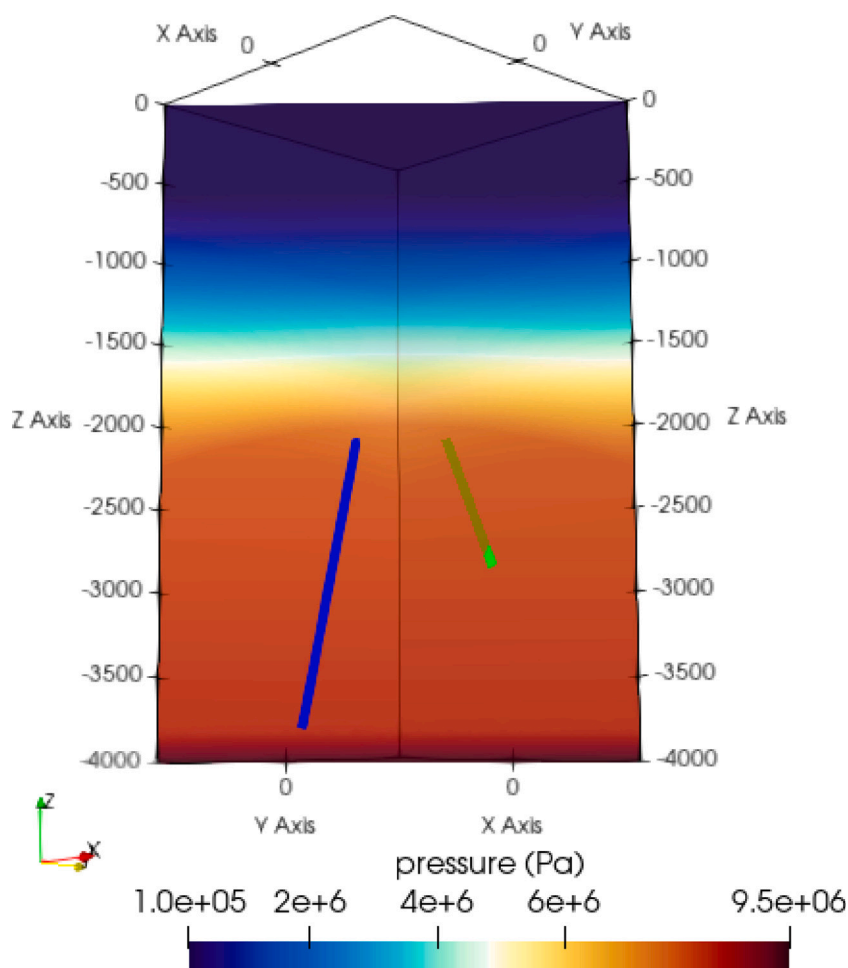


Fig. 13. Pressure distribution at the initial state of the steam-dominated reservoir.

3.1.5. Global description of the results

Fig. 6 displays the temporal evolution of the temperature field induced by exploitation near the production area (left) and the gas saturation (right) at different time steps (0, 2, 3.1, and 20 years).

In early stages of production (i.e. prior to the start of injection), the depletion around the producer well favors the formation of a steam cap in both the reservoir and the fault zones (Fig. 6.b.). As fluid is produced from the reservoir, the pressure and temperature decrease, resulting in the formation of steam within the reservoir. The steam accumulates at the top of the reservoir and in the fault zones where the gas saturation is maximum. However, since the caprock part of the faults is not completely sealed, slight steam migration occurs toward the surface through faults (Fig. 6.b.).

The start of injection induces an increase in reservoir pressure and a steam cap contraction while steam around the injector condenses (Fig. 6.c. vs. Fig. 6.d.). Impact of the reinjection on the steam cap is very quick with the vapor cloud almost disappearing in 1 month (Fig. 6.d.).

After 20 years of production, only a small fraction of steam can be observed in the reservoir near the producer. Note that the upflowing plume, which is delineated by the isotherm surface of 250 °C, has been impacted by the injection of colder fluid. Its extension is clearly reduced in comparison with the natural state (Fig. 6.d.).

The re-injection of fluid at a flow rate of 144 ton h⁻¹ (80% of the production) provides an efficient pressure support and allows to maintain conditions close to the natural state with the vast majority of the reservoir stabilized in liquid state.

3.1.6. Focus on the producer well

Figs. 7, 8, 9 and 10, respectively display the evolution of pressure, specific enthalpy, gas saturation and temperature of the produced fluid in the producer well at a depth equal to that of the reservoir top and in the reservoir at the same depth, over a period of 10 years.

In the early stages of production, pressures (in the well and in the reservoir at the top depth) decline rapidly (Fig. 7) and result in the production of steam in the well, the gas saturation in the well reaches its maximum value (around 0.9) after half a year (Fig. 9). Simultaneously the temperature of the produced fluid decreases from 245 °C to around 220 °C (Fig. 10), due to the cooling effect of the vaporization. In the meantime, the well specific enthalpy reaches around 1150 kJ/kg, which is higher than the natural state values (Fig. 8) in the reservoir. This excess enthalpy can be explained (Zarrouk and McLean, 2019) by, on one hand, the higher mobility of steam compared to liquid water and on the other hand by an enhanced vaporization of the boiling water in the fractures near the well, ensured by diffusive heat flow from the matrix rock to the fracture fluid. This phenomenon is obviously transient and a decline of the produced fluid enthalpy is then observed (Fig. 8) in conjunction with a slight well gas saturation decrease (Fig. 9). Indeed, if the pressure produced by a discharging well is sufficient to cause boiling in the producing aquifer, it is common that the discharge enthalpy of the well to exceed the enthalpy of the aquifer fluid beyond the zone of depressurization around the well. This phenomenon has been reported and studied for different geothermal sites worldwide, with numerous studies delving into its underlying principles and concepts (Truedsdell, 1979; Grant et al., 1984; Arnorsson et al., 2010; Angcoy and Arnorsson, 2011; Egbert et al., 2021; Sandström, 2021).

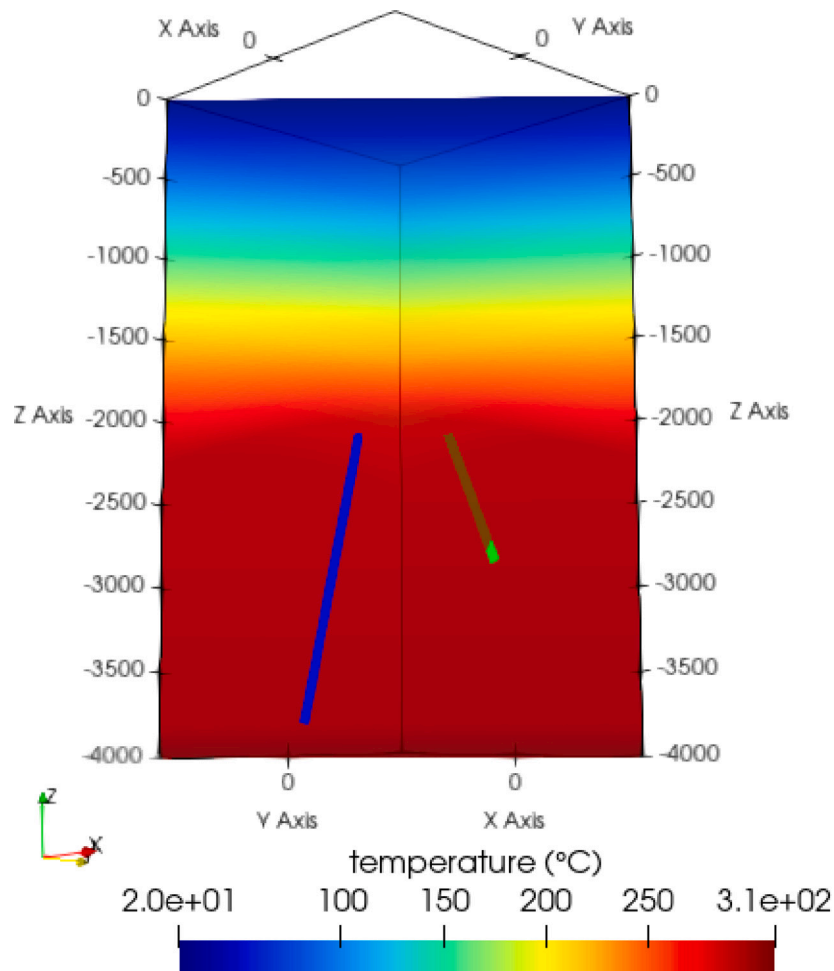


Fig. 14. Temperature ($^{\circ}\text{C}$) distribution at the initial state of the steam-dominated reservoir.

During this period, the hot steam cloud migrates upward to the top of the reservoir where temperature increases (orange curve in Fig. 10) and steam accumulates over time (Fig. 6.b.). This steam cap expansion at the top of the reservoir is characterized by gas saturation reaching its maximum values after two years. Then it decreases due to the decline in boiling (dark red curve in Fig. 9), while the reservoir temperature and pressure are maintained at constant values (Figs. 7 and 10).

After the injection starts, the producer is quickly impacted due to pressure build-up (Fig. 7) which results in a rapid decrease of gas saturation (around 15%, Fig. 9) and an increase of the temperature of the fluid produced in the well (Fig. 10) and a quick decline of the fluid enthalpy (Fig. 8). From this moment on, operating conditions remain relatively stable.

3.2. Steam-dominated reservoir

3.2.1. Context, objective and geometry

This section investigates the behavior of a steam dominated reservoir with full reinjection of the produced fluid. The modeled domain measures $2\text{ km} \times 2\text{ km} \times 4\text{ km}$ and consists of a reservoir that is 2 km thick, covered by a 2 km thick caprock (respectively blue and yellow domains in Fig. 11). The upper boundary of the reservoir is modeled as a curved surface with a concave shape. The geothermal field is operated with two deviated wells: a steam producer open in the upper section of the reservoir (green in Fig. 11) and an injector which crosses the whole reservoir (blue in Fig. 11).

3.2.2. Hydraulic and thermal properties

The reservoir is assumed to have homogeneous 0.035 porosity and 10^{-14} m^2 permeability, while the thick overburden has lower values (0.015 porosity and 10^{-20} m^2 permeability). The rock thermal properties and densities are constant for the whole rock mass with thermal conductivity $\lambda = 2\text{ W K}^{-1}\text{ m}^{-1}$, specific heat capacity $c_p = 1000\text{ J kg}^{-1}\text{ K}^{-1}$, and density $\rho_{rock} = 2600\text{ kg m}^{-3}$.

3.2.3. Initial and boundary conditions

As a preliminary step, the geothermal system's natural state is obtained by performing a simulation for 10,000 years with the caprock assumed to be initially in a liquid phase, with hydrostatic pressure (atmospheric pressure on top), and a temperature field increasing linearly with depth (from $30\text{ }^{\circ}\text{C}$ at the top to $280\text{ }^{\circ}\text{C}$ at the bottom). The reservoir is assumed to be initially two-phase with constant temperature ($T_{res} = 295\text{ }^{\circ}\text{C}$) and gas saturation ($S_g = 0.9$). Dirichlet boundary conditions are used for temperature and pressure at the top surface (with $T_{top} = 20\text{ }^{\circ}\text{C}$ and $P_{top} = 1\text{ bar}$), and a high heat flux of 275 mW m^{-2} is imposed at the bottom boundary (Neumann boundary condition). No flow conditions are applied on the lateral boundaries.

In its natural state, the geothermal system is characterized by a liquid zone at the bottom of the reservoir, while the remaining part of the reservoir is gas dominated. The caprock is in liquid state (Fig. 12). The pressure in the caprock is hydrostatic, while the pressure in the reservoir is approximately 80 bars (Fig. 13). The temperature within the caprock increases linearly with depth and remains constant at around $300\text{ }^{\circ}\text{C}$ over the convective part of the reservoir (Figs. 14 and 16).

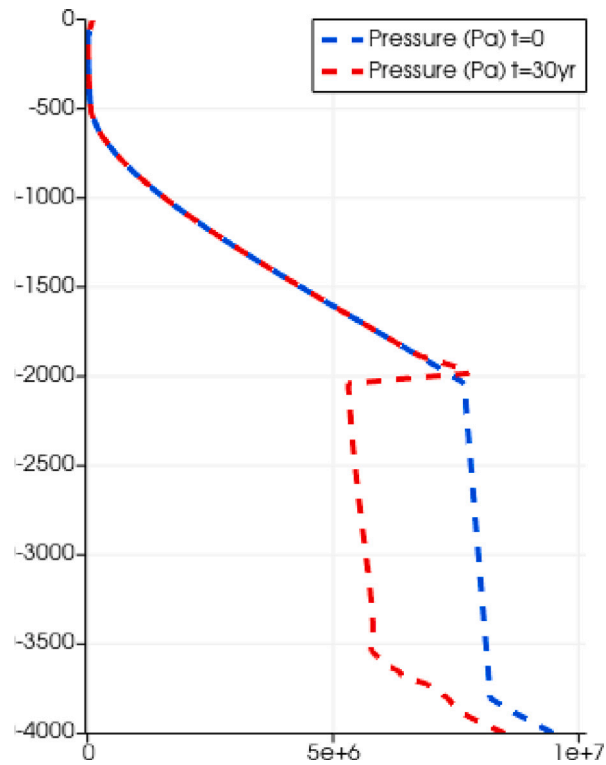


Fig. 15. Vertical pressure profiles (passing through the base of the injection well) — blue: initial pressure — red: after 30 years of production.

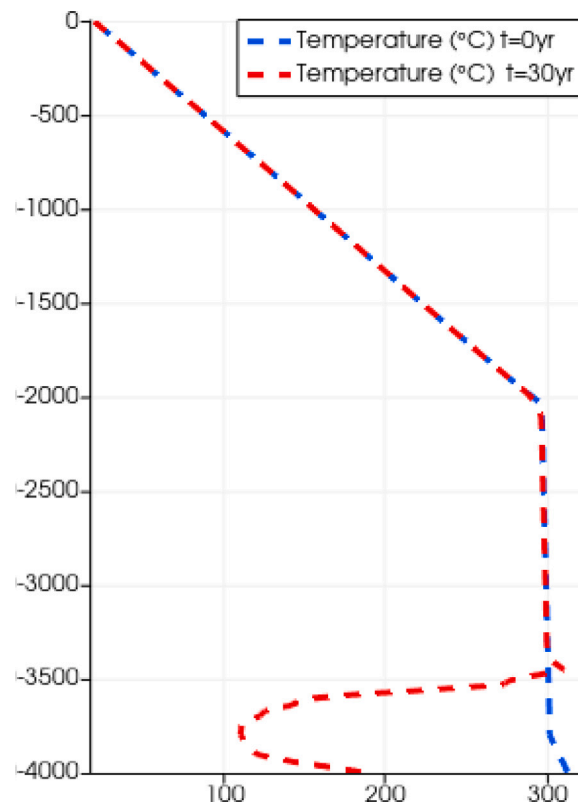


Fig. 16. Vertical temperature profiles (passing through the base of the injection well) — blue: initial temperature — red: after 30 years of production.

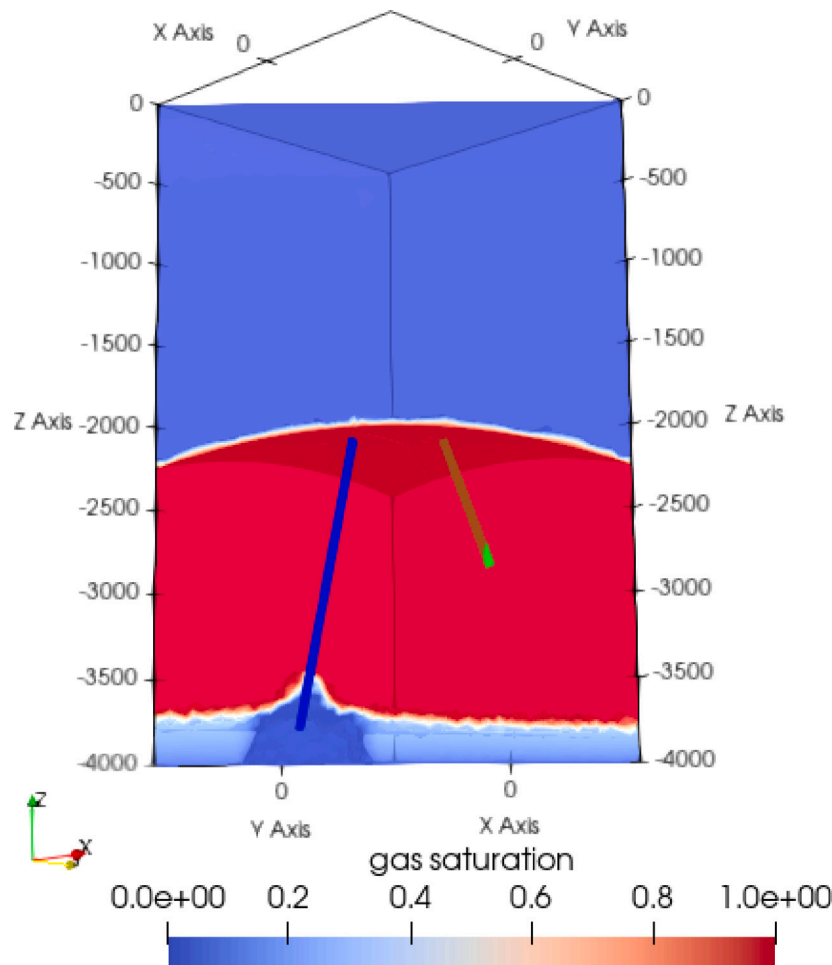


Fig. 17. Gas saturation within the reservoir after 30 years of production.

3.2.4. Exploitation scenario

A constant flow rate of 75 ton h^{-1} is used to produce the reservoir during 30 years. The condensed fluid is fully reinjected at the wellhead with a temperature of $110 \text{ }^\circ\text{C}$. Boundary conditions remain the same as for the natural state computation.

Figs. 17–19 respectively show the distribution of gas saturation, pressure and temperature at the end of the exploitation period. A liquid cone has formed at the base of the injection well, which has favored the condensation of steam around the injector. Figs. 15 and 16 display the vertical profiles of pressure and temperature passing through the base of the injection well, at both initial and final time.

After 30 years of production, the steam pressure has decreased by approximately 23 bars, while the gas–liquid interface has risen due to the reinjection of cold fluid.

4. Conclusions and perspectives

We propose a geothermal reservoir 3D modeling workflow based on the use of unstructured conformal meshes to capture the geometries of geological objects (formation interfaces, faults or fractures) or industrial devices (well paths). This choice requires to use an mixed-dimensional model and adapted numerical schemes. Among such schemes, we selected the Vertex Approximate Gradient finite volume scheme which can handle generic polyhedral meshes and has been adapted to mixed-dimensional multi-phase multi-component

flows. Moreover, its computational cost depends on the number of vertices of the mesh which makes it particularly interesting for tetrahedral meshes. A parallel version of the VAG scheme was implemented in the ComPASS code with a mixed dimensional multi-phase multi-component physical model relying on a natural variables (*a.k.a.* Coats) formulation. A simple well model, can then be used to simulate geothermal reservoir exploitation scenarios. This capacity has been demonstrated on two case studies inspired for real-world high-energy geothermal fields.

In ComPASS version 4, which has been used in this work, a lot of effort has been put in designing a Python API which is not a simple pre- or post-processing layer. Thanks to it, the user is given the possibility of a fine-grained interaction with the numerical workflow, without loss of performance or the need for (re-)compilation. Then, building on the power of the Python ecosystem, complex exploitation workflows can be simulated (cf. simulation scripts used in Section 3). The current development efforts focus on different aspects. The well model has been extended to multi-segmented wells with slip velocity between phases, cross-flows, and wall friction and was introduced in ComPASS v4 (Armandine Les Landes et al., 2023). Several physics are developed taking advantage of the generic thermodynamic framework. A diphasic (air–water) module was used to model interactions of an hydrosystem with precipitations (Burnol et al., 2023) whereas specific boundary conditions were developed to take into account exchanges with the atmosphere (Beaude et al., 2019). Additionally, a specific equation of state is currently developed for gas mixtures (Ben Rhouma et al., 2022).

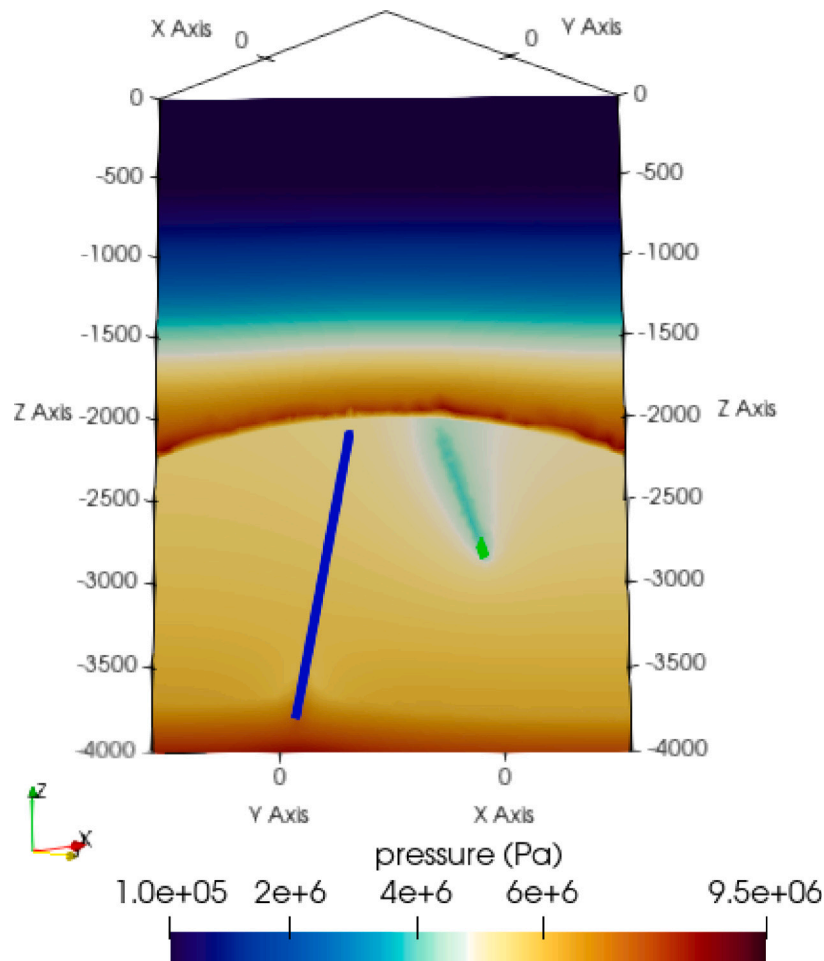


Fig. 18. Pressure distribution within the reservoir after 30 years of production.

Finally, version 5 of ComPASS will consist in a modular refactoring of ComPASS with the overall objective of being able to use simultaneously classical TPGA schemes and more complex scheme such as the VAG scheme (Beaude, 2018).

CRediT authorship contribution statement

A. Armandine Les Landes: Writing – original draft, Review & editing, Simulations, Visualization, Meshing, Investigation. **L. Beaude:** Code developer, Model description, Writing – review and editing. **D. Castanon Quiroz:** Well model development, Writing – review and editing. **L. Jeannin:** Supervision, Project administration, Writing – review and editing, Investigation. **S. Lopez:** Code developer, Model description, Investigation, Writing – original draft, Review & editing, Project administration. **F. Smai:** Code developer. **T. Guillon:** Meshing, Code developer. **R. Masson:** Theoretical formalism and early versions of the code, Writing - review and editing, Investigation..

Code availability

ComPASS is co-developed by BRGM and Université Côte d'Azur (LJAD - Inria) and licensed under GPLv3.

The code is versioned using gitlab. Version 4, which was used in this work, is freely available at: <https://gitlab.com/compass/compass-v4/compass>.

The corresponding online documentation can be found at: <https://charms.gitlabpages.inria.fr/ComPASS>.

As of today the code runs under Linux OS (possibly through docker or WSL on Windows host system).

To make the installation step smoother we provide a tailored conda environment.

All scripts used to run the simulations presented in Section 3 are available on the [gitlab platform](https://gitlab.com).

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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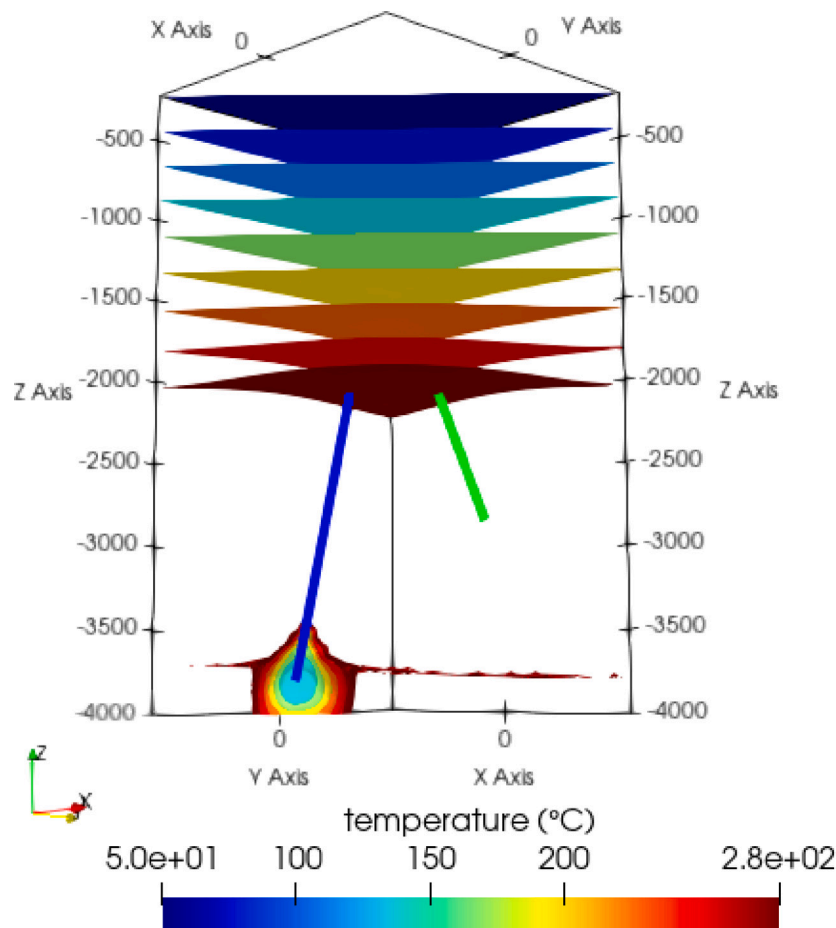


Fig. 19. Temperature distribution (°C) within the reservoir after 30 years of production.

Data availability

No data was used for the research described in the article.

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