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# Examining the contribution of near real-time data for rapid seismic loss assessment of structures

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## Abstract

This study proposes a probabilistic framework for near real-time seismic damage assessment that exploits heterogeneous sources of information about the seismic input and the structural response to the earthquake. A Bayesian network is built to describe the relationship between the various random variables that play a role in the seismic damage assessment, ranging from those describing the seismic source (magnitude and location) to those describing the structural performance (drifts and accelerations) as well as relevant damage and loss measures. The *a priori* estimate of the damage, based on information about the seismic source, is updated by performing Bayesian inference using the information from multiple data sources such as free-field seismic stations, global positioning system receivers and structure-mounted accelerometers. A bridge model is considered to illustrate the application of the framework, and the uncertainty reduction stemming from sensor data is demonstrated by comparing prior and posterior statistical distributions. Two measures are used to quantify the added value of information from the observations, based on the concepts of pre-posterior variance and relative entropy reduction. The results shed light on the effectiveness of the various sources of information for the evaluation of the response, damage and losses of the considered bridge and on the benefit of data fusion from all considered sources.

## Keywords

Bayesian networks, Bayesian updating, multisensory data fusion, probabilistic seismic demand modelling, structural health monitoring

## Introduction

The rapid assessment of the ground-shaking intensity and damage distribution in the aftermath of a major earthquake is of paramount importance for ensuring a timely emergency response, accurate loss estimation, and for providing accurate information to the public. It enables emergency management authorities to take action immediately after the earthquake and correctly allocate and prioritize resources to minimize further casualties and speed up recovery from disruption.<sup>1</sup>

ShakeMaps have proven to be very effective tools for rapidly responding to earthquakes.<sup>2</sup> They are contour maps of several ground-motion parameters (also called intensity measures), such as peak ground acceleration and pseudo-spectral acceleration at different system periods estimated using empirical ground-motion prediction equations (GMPEs) based on information on the earthquake source (magnitude and location) and instrumental data from available seismic stations. Some examples of similar approaches include

works by Gehl et al.,<sup>3</sup> Michelini et al.<sup>4</sup> and Bragato.<sup>5</sup> ShakeMap information can also be combined with vulnerability curves (e.g. those provided by HAZUS<sup>6</sup>) for structural damage estimation in an area (see, for instance, the studies by Wald et al.<sup>2</sup> and Lagomarsino et al.<sup>7</sup>).

Structural health monitoring (SHM) systems have also been proven to provide useful information for rapid seismic damage assessment<sup>8,9</sup>. Most existing SHM methodologies rely on the use of vibration measurements through accelerometers to detect potential

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structural damage.<sup>10</sup> Encouraged by the recent technological developments in the field, global positioning system (GPS) receivers have also been increasingly used for damage detection.<sup>11–14</sup> Yet, associating damage with dynamic features is heavily restrained by the instrumentation layout/specifications, environmental effects and even the algorithms or methods used.<sup>15–18</sup> In addition to the specific sensing techniques focussed on a particular physical parameter, there are recent applications that make use of the multisensory environment and heterogeneous data for SHM.<sup>19</sup> This can take the form of converting sensor information from one domain to another for corrected or enhanced<sup>20–22</sup> dynamic characterization, seeking changes in vibration behaviour as indicators of damage.

Seismic damage assessments should be carried out with probabilistic approaches, given the many uncertainties inherent to the problem. For example, even if the earthquake location and magnitude are known with good accuracy, significant uncertainty stems from the use of GMPEs.<sup>23–27</sup> Moreover, SHM sensor measurements are affected by noise, errors and have limited accuracy. Acknowledging the important role of uncertainties, in recent years an increasing number of studies have combined SHM and performance-based earthquake engineering (PBEE) concepts for rapid quantification of earthquake-induced building losses.<sup>8,28–30</sup>

Bayesian modelling is a natural choice for carrying out rapid earthquake damage assessments, as it permits the propagation of uncertainties through models and allows updating the *a priori* estimates when new information becomes available. In particular, Bayesian networks (BNs) are ideal tools for describing the probabilistic relationships between the various parameters involved in the damage assessment and for integrating the available knowledge of the earthquake scenario and the structural response. In this context, Bayraktarli et al.,<sup>31</sup> Bensi,<sup>32</sup> Broglio et al.<sup>33</sup> and Gehl<sup>34</sup> proposed BN frameworks for risk assessment of urban infrastructure systems. Wu<sup>35</sup> developed a Bayesian framework for estimating the seismic damage in a structural system both before and after an earthquake, combining earthquake early warning and SHM data. Bayesian modelling can also be useful for quantifying the added value of the information provided by sensors and monitoring systems.<sup>36–40</sup> Approaches commonly employed for quantifying the reduction of uncertainty due to the available information are based on the concept of pre-posterior variance<sup>36,40–42</sup> or relative entropy reduction.<sup>43</sup>

In this article, a probabilistic framework based on BNs is developed to quantify the benefit of various sensors for seismic damage assessment of critical structures under earthquake loading. The proposed framework relies on heterogeneous sources of information, such as

those provided by seismometers typically used for deriving ShakeMaps, structure-mounted accelerometers and GPS receivers. The framework is applied to evaluate the seismic damage of a two-span bridge model located in a zone of high seismicity. To the authors' knowledge, this is the first time that heterogeneous sensing techniques are used in a BN framework to update the estimates of the seismic losses of a system, and that the effectiveness of these sensing techniques is compared by using the pre-posterior variance and relative entropy reduction metrics.

The section 'Seismic damage assessment' illustrates in detail the various stages of the seismic damage assessment, the parameters involved and the technologies that are available to measure them. The section 'Bayesian framework' illustrates the BN developed to describe the relationship between the various parameters involved in the seismic damage assessment, and to update these parameters based on additional available information from different sources. It also presents the alternative approaches for quantifying the uncertainty reduction stemming from the sensor data. The section 'Case study' illustrates the implementation of the method on the two-span bridge considered as a case study. This is followed by a discussion of the results and the conclusion.

## Seismic damage assessment

The Bayesian framework for seismic damage assessment combines four types of analyses, namely hazard analysis, structural analysis, response analysis and loss analysis, which is consistent with PBEE frameworks.<sup>44,45</sup> Since the focus of this study is the rapid damage assessment in the aftermath of an earthquake, the first stage is replaced by the assessment of the level of shaking at the site, given that the main characteristics of the earthquake are known. The subsequent subsections describe in more detail the four analysis stages, together with the involved parameters and the technologies for measuring them.

### Seismic shaking analysis

This analysis provides an estimate of the probabilistic distribution of a given ground-motion parameter or intensity measure (*IM*) at the site of interest given the following variables that are assumed to be known: the moment magnitude of the earthquake ( $M_w$ ); the epicentre of the earthquake, if a point-source event is assumed, or the rupture location and its extent for finite-fault scenarios; and other parameters characterizing the fault such as the faulting mechanism, the fault geometry and the depth to the top of the rupture. The analysis is carried out following the Bayesian procedure

developed by Gehl et al.<sup>3</sup> for generating ShakeMaps. A GMPE is used to estimate the ground motion at the site, given the earthquake's characteristics. The GMPE is generally characterized by the following form<sup>23</sup>

$$\log(IM_i) = f(M_w, R_i, \mathbf{s}) + \eta + \zeta_i \quad (1)$$

where  $f(M_w, R_i, \mathbf{s})$  is a function describing the lognormal mean of  $IM_i$ , that is, the  $IM$  at the location  $i$ , based on the earthquake magnitude  $M_w$ , a measure of the source-to-site distance  $R_i$  and other parameters collected in the vector  $\mathbf{s}$ ;  $\eta$  is the inter-event (or between-event) error term from the GMPE; and  $\zeta_i$  is the intra-event (or within-event) error term from the GMPE.

The interevent error term describes the systematic variability in the ground motions throughout the region produced by different earthquakes of the same magnitude and rupture mechanism. The intra-event error describes the variability in ground-motion intensity at various sites of same soil classification and distance from the source during a single earthquake.<sup>24</sup> Thus, following the studies by Park et al.<sup>25</sup> and Crowley et al.,<sup>26</sup> the same interevent variability is applied to all sites of interest within a given earthquake scenario, whereas the intra-event variability is represented by a spatially correlated Gaussian random field. This can be built based on the intra-event error terms  $\zeta_i$  and the correlation coefficient  $\rho_{ij}$  between the ground-motion parameters at two sites  $i$  and  $j$ , for  $i, j = 1, 2, \dots, N_{sites}$ , where  $N_{sites}$  is the number of sites of interest. The corresponding covariance matrix of the ground-motion  $IM$  field has the following form

$$\Sigma_{IM} = \begin{bmatrix} \sigma_\eta^2 + \sigma_\xi^2 & \cdots & \sigma_\eta^2 + \rho_{ij}\sigma_\xi\sigma_\xi \\ \vdots & \ddots & \vdots \\ \cdots & \cdots & \sigma_\eta^2 + \sigma_\xi^2 \end{bmatrix} \quad (2)$$

where  $\sigma_\eta$  and  $\sigma_\xi$  represent the standard deviations of the inter- and intra-event error terms, respectively, provided by the GMPE. Further details about this representation of the ground-motion field can be found in the study by Gehl et al.<sup>3</sup> and in Schiappapietra et al.<sup>46</sup>

The field observations of the ground-motion parameters at seismic stations can be used as evidence to update the prior estimates of the  $IM$  at the site of interest. The spatial correlation structure between the  $IM$ s at the monitored points and at the site plays a major role in the propagation of the observations.<sup>47</sup>

### Structural analysis

Structural analysis is performed to estimate the probabilistic distribution of one or more engineering demand parameters ( $EDPs$ ), describing the response of structural and non-structural components, based on

the seismic shaking intensity. A joint probabilistic seismic demand model should be considered to describe the relationship between the  $EDPs$  and the  $IM$ , by also accounting for the correlation between the various  $EDPs$ . This is very important because the correlation structure is a basis for updating the probabilistic distribution of one  $EDP$  (e.g. floor acceleration in a building) given the observation of another (e.g. storey drift).

Alternative approaches can be employed to develop the joint probabilistic seismic damage model (PSDM), such as multi-stripe analysis,<sup>48</sup> incremental dynamic analysis,<sup>49</sup> or cloud analysis.<sup>50</sup> In this study, cloud analysis is adopted. For this purpose, the structural model is analysed under a set of ground-motion records of different  $IM$  levels. The samples of the various response parameters ( $EDP_i$ , for  $i = 1, 2, \dots, N_{EDP}$ ) are then fitted by a regression model. In particular, a bilinear model is considered in this study,<sup>51,52</sup> since it allows a better description of the evolution of the structural response with the seismic intensity. The model for the generic  $i$ th  $EDP$  has the following form (see Figure 1)

$$\begin{aligned} \ln(EDP_i|IM) = & [a_1 + b_1 \ln(IM) + \ln \varepsilon_1] H(IM - IM^*) \\ & + [a_1 + b_1 \ln(IM^*) + b_2(\ln(IM) - \ln(IM^*)) + \ln \varepsilon_2] \\ & [H(IM^* - IM)] \end{aligned} \quad (3)$$

in which  $a_1$  is the intercept of the first segment,  $b_i$  for  $i = 1, 2$  are the slopes of the two segments (see Figure 1),  $IM^*$  is the breakpoint  $IM$ , which is defined as the point of intersection of the two segments. The step function  $H(g)$  controls which of the two segments must be considered (i.e.  $H = 0$  for  $IM \leq IM^*$  and  $H = 1$  for  $IM > IM^*$ ). The probability distribution of each  $EDP$  is also described by the values of the error functions  $\varepsilon_i$ , which are characterized by a lognormal distribution with lognormal zero mean and lognormal standard deviations  $\beta_i$ . Moreover, in order to define a joint probability density function (PDF) for the various  $EDPs$ , a covariance matrix must be assigned, which has

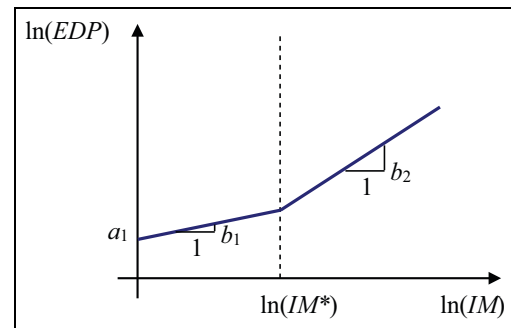


Figure 1. Illustration of the bilinear regression model.

**Table 1.** Engineering demand parameters and measurement possibilities.

EDP	Component performance	Direct measurement	Indirect measurement
Peak transient displacement ( <i>TD</i> )	Global structural components, non-structural components	GPS receivers, laser vibrometer, transducers, camera	Accelerometers
Residual displacement ( <i>RD</i> )	Global structural components	GPS receivers, laser vibrometer, transducers, camera	Accelerometers
Peak absolute acceleration ( <i>PA</i> )	Non-structural building components, bridge deck	Accelerometers	GPS receivers

EDP: engineering demand parameter; GPS: global positioning system.

the same form as that of equation (2). For this purpose, different correlation coefficients must be estimated for the two conditions corresponding to  $IM \leq IM^*$  and  $IM > IM^*$ , thus leading to two correlation matrices,  $\sum_{EDP}^I$  and  $\sum_{EDP}^{II}$ .

A brief description of the *EDPs* considered in this study and relevant measurement techniques is given below. Table 1 summarizes the *EDPs* of interest and possible sensors to collect observations directly and indirectly.

**Peak transient displacements.** The maximum absolute values of the transient displacements (or of geometrically derived quantities, such as drifts) during the time history of motion of a structure are important indicators of structural performance. Many vulnerability curves for structures are based on these *EDPs*. Peak transient displacements (*TDs*) can be derived from the time histories of structures' relative displacements with respect to the base, and a wide range of sensors (both contact and non-contact) can be used to measure them.

Lemnitzer et al.<sup>53</sup> employed transducers such as linear variable differential transformers (LVDTs) to measure the shear deformations of a wall across two floors of a building, whereas Li et al.<sup>54</sup> proposed the use of smartphone cameras. Trapani<sup>55</sup> developed SAFEQUAKE, a hinged bar instrumented with two bi-axial accelerometers measuring accelerations, one at each end of the beam and remaining parallel to the building floors, and one bi-axial inclinometer or accelerometer measuring the tilt of the beam. There are also some applications of GPS systems for real-time monitoring of displacement measurements. However, GPS technology is limited by low sampling rates and because it only measures the displacements at the building roof or bridge deck level.<sup>56</sup>

**Residual displacements.** The residual drift or permanent deformations of structural components after the earthquake may be used to infer the degree of damage sustained by the structure. Many studies have investigated

the correlation between maximum drifts and residual displacements (*RDs*; see study by Dai et al.<sup>57</sup> for a recent review on the topic). However, most of these studies have aimed at developing empirical formulae to relate the *RDs* and *TDs* and to provide a deterministic relation between the two *EDPs*, without any information regarding the dispersion<sup>58</sup> nor any consideration of its dependence on the seismic intensity. Probabilistic studies relating *TDs* and *RDs* or drifts are scarce. Goda<sup>59</sup> developed a joint PDF for the probability distribution of *TD* and *RD* seismic demands using a copula. Ruiz-García and Miranda<sup>60</sup> evaluated and compared demand hazard curves for residual drifts and maximum transient drifts in multi-storey building frames. Uma et al.<sup>61</sup> developed a probabilistic performance-based seismic assessment framework where the performance levels defined by pairs of maximum-residual deformations are derived using bivariate probability distributions. Yazgan and Dazio<sup>62</sup> proposed a Bayesian approach for post-earthquake damage assessment using the information from known *RDs* to update the probability distribution of maximum transient drifts in building frames.

**Peak absolute accelerations.** Many non-structural components in buildings are damaged during earthquakes when subjected to large absolute acceleration demands rather than high drift demands. Suspended ceilings, parapets and light fixtures are typical building components sensitive to accelerations. Along with masonry infills, ceiling systems are the non-structural elements most prone to damage during an earthquake. Absolute accelerations are typically measured via accelerometers. Accelerations may also be derived by differentiating velocities and displacements but obtaining reliable estimates can be problematic unless smooth velocity or displacement signals with high sample rates are available.

Excessive bridge accelerations can cause serviceability problems, and in case of an earthquake, may distort operational flow (e.g. driver safety<sup>63</sup>). Although mostly disregarded, vertical bridge accelerations can sometimes

be excessive and may necessitate external devices for control.<sup>64</sup>

### Damage analysis

In this stage, the *EDPs* are used to estimate the level of damage of the structure, typically described by one or more damage states (*DSs*). In buildings, damage of structural components can be described as a function of the peak inter-storey drift ratio, and that of non-structural components based on the peak absolute accelerations (*PAs*).<sup>29,65</sup> In bridges, the damage of the bearings, shear keys, columns and abutments is controlled by kinematic quantities, such as displacements and curvatures. Bridge piers are often the most vulnerable components of a bridge<sup>66,67</sup> and their damage can be expressed as a function of the peak drift ratio<sup>68</sup> or it can be related to the maximum displacement ductility experienced.<sup>69,70</sup>

### Loss analysis

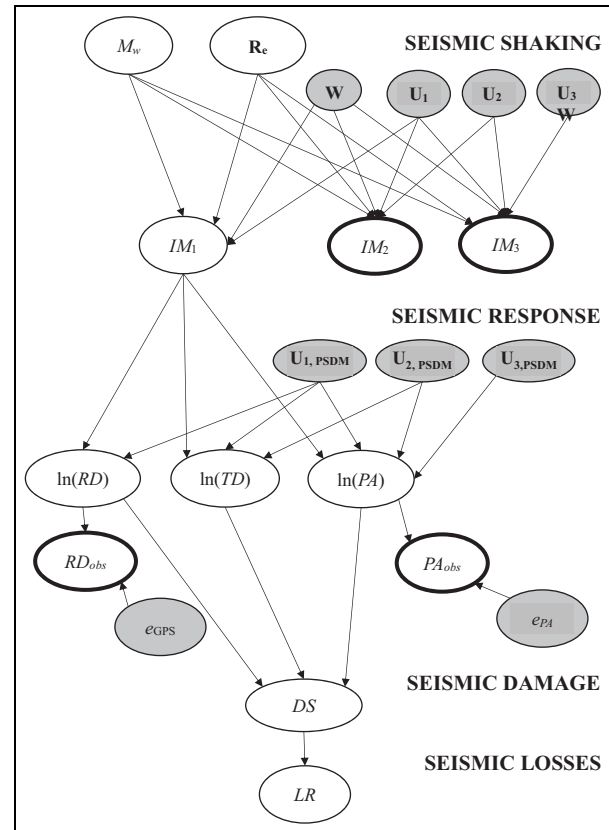
In this final stage, various decision variables (*DVs*) can be calculated, such as repair cost, casualties and loss-of-use duration (money, deaths and downtime), based on the damage sustained by the structural components. Padgett et al.<sup>71</sup> after Basöz and Mander<sup>72</sup> associated loss levels with damage measures experienced by bridges. Lu et al.<sup>73</sup> pursued a similar loss assessment scheme for buildings with multi-class damage descriptions. Similar to these studies, in this article, structural losses related to damage are formulated in terms of loss ratios (*LRs*), repair and replacement costs normalized by the bridge cost.

## Bayesian framework

This section presents the Bayesian framework developed for near real-time loss assessment and describes the methods used for quantifying the effectiveness of sensors for uncertainty reduction.

### Bayesian network

This subsection illustrates the BN developed to describe the probabilistic relationship between the parameters specified in the previous section, to perform predictive analysis and to update these parameters based on additional information from different observations (see Figure 2). The magnitude  $M_w$  and epicentre of the earthquake are assumed to be known, and three different types of information are assumed to be available to update the probabilistic relationship of the variables in the network: on-site seismometers located close to the site of the structure, providing information on *IM* levels; GPS data, updating the knowledge of the *RD*; and



**Figure 2.** Bayesian network illustrating the relationship between the parameters involved in the damage and loss assessment (observed quantities indicated with thick lines).

accelerometer data, updating the knowledge of the *PA* in the bridge deck.

The nodes of the BN represent random variables characterized by a PDF. In particular, nodes are related to their parent and child variables through edges stating conditional dependencies between variables (i.e. use of conditional probability distributions). The nodes that have no parents are termed as root nodes and they are associated with marginal probability distributions. Node junction patterns can take different forms such as collider ( $M_w$  and  $R$  to  $IM$ ), fork ( $IM$  to *EDPs*) and chain ( $TD$  to damage, damage to loss) with varying dependency features. Two forms of probabilistic inference can be carried out in BNs: predictive analysis that is based on evidence (i.e. information that the node is in a particular state) on root nodes and diagnostic analysis, also called Bayesian learning, where observations enter into the BN through the child nodes. When evidence enters the BN, it is spread inside the network thereby updating the probability distribution of the variables through one of the two forms of inference mentioned above.

The seismic shaking is modelled by the deterministic root nodes that describe the magnitude of the

earthquake event,  $M_w$ , and the vector  $\mathbf{R}_e$  that collects the distances between the source and the site, and the source and the seismic stations. For demonstration purposes, two seismic stations (represented by  $IM_2$  and  $IM_3$ ) are assumed here to be in the vicinity of the bridge site (represented by  $IM_1$ ).

Following the study by Gehl et al.,<sup>3</sup> the interevent variability is modelled by the root node  $W$ , which is parent to the three  $IM$ s of interest (i.e. the one at the site and the ones at the seismic stations) and follows a normal standard distribution. The intra-event variability is modelled via three root nodes,  $U_j$ , for  $j = 1, 2, 3$ , which also follow a normal standard distribution. The joint conditional distribution of the  $IM$ s, given  $W$  and  $U_i$ , can be expressed by the following relation

$$\ln(IM_i|W, U_j) = \ln \overline{IM}_i(M_w, R_i) + \sigma_\xi \sum_{j=1}^3 t_{ij} U_j + \sigma_\eta W \quad (4)$$

$i = 1, 2, 3$

where  $\overline{IM}_i$  is the median value of the  $IM$  and  $\ln \overline{IM}_i(M_w, R_i)$  is the lognormal mean, which is a function of  $M_w$  and  $R_i$  (see also equation (1));  $\sigma_\xi$  and  $\sigma_\eta$  are the lognormal standard deviations describing, respectively, the intra-event and interevent variability;  $t_{ij}$  is a term of the lower triangular matrix obtained through a Cholesky factorization of  $\mathbf{C}_{IM}$ , which is the spatial correlation matrix expressing the correlation between the  $IM$ s at the various sites.

A similar approach is used for the PSDM describing the conditional distribution of the  $EDPs$  given the  $IM$  at the site,  $IM_1$ . However, in this case, a bilinear model is employed, and thus two different error variables and correlation matrixes have to be considered, one for  $IM_1 < IM^*$  and the other for  $IM_1 > IM^*$ . Two other root nodes, denoted as  $e_{GPS}$  and  $e_{ACC}$ , are used to describe the measurement errors of the observations obtained with GPS and accelerometers. These error variables are assumed to be zero-mean normally distributed variables. Finally, a damage model is employed to describe the conditional relationship between the various  $DS$ s of the system and the  $EDPs$ , and a loss model to relate the losses to damage.

The BN detailed in Figure 2 is used to perform predictive analysis, starting from the prior distribution of the root nodes, and diagnostic analysis, entering an observation at the nodes  $IM_2$ ,  $IM_3$ ,  $RD_{obs}$  and  $PA_{obs}$ . For this purpose, the OpenBUGS software<sup>74</sup> is employed, which is interfaced with the R statistical tool. OpenBUGS is able to treat both deterministic (e.g.  $M_w$  and  $\mathbf{R}_e$ ) and probabilistic (e.g.  $IM_i$ ,  $\ln(TD)$ ) variables, which are sampled through a Markov-chain Monte-Carlo (MCMC) sampling scheme. Each chain is built with a Gibbs sampling scheme, where variables

are successively sampled from the posterior distribution of previous variables: the posterior distribution of a variable is obtained from the product of the prior distribution and the likelihood function (probability of a given observation occurring given the prior distribution). The samples are then aggregated in order to estimate empirical statistics of the variables of interest, which represent the posterior distributions. Although Bayesian inference based on sampling provides only approximate solutions (i.e. the posterior distribution is built from the samples), it has the benefit of being much more flexible than exact inference algorithms such as junction-tree inference (e.g. it allows modelling continuous variables using various probability distributions). Due to the approximate nature of the posterior distributions sampled by the MCMC scheme, there is no absolute guarantee that exact distribution parameters may be obtained. However, various steps may be taken in order to ensure a reasonable accuracy of the results:

- Generation of multiple MCMC chains starting with different combinations of initial conditions, in order to ensure that all chains end up converging towards the same values.
- Generation of a high number of samples for each chain (e.g. several tens of thousands).
- Definition of a ‘burn-in phase’, where the first part of each chain is taken out from the estimation of the posterior distribution, in order to remove samples that have not yet converged.
- Thinning of the samples (i.e. only one sample in every five is considered in each chain), in order to reduce autocorrelation effects that are inherent to MCMC sampling.

Specific statistical tools in OpenBUGS are dedicated to the estimation of auto-correlation and of the minimum number of samples. In any case, preliminary tests are necessary to calibrate the sampling parameters carefully. The chosen sampling results from a trade-off between the required accuracy level and the computational cost.

### Quantification of sensors’ effectiveness for uncertainty reduction

**Pre-posterior variance.** The effectiveness of the monitoring strategy can be described based on the concept of pre-posterior variance,<sup>41</sup> which represents the expected value of the variance of the random variable of interest (e.g.  $EDP$ ) after monitoring is performed, that is, after Bayesian updating is carried out based on the available information. The pre-posterior variance accounts for

all the possible combinations of outcomes of the monitoring system and thus it is independent of any specific observation. Compared with the prior variance, the pre-posterior variance gives an idea of how useful the monitoring process is in gaining information on the unknown parameter. A pre-posterior variance much smaller than the prior indicates that the proposed monitoring method improves our knowledge of the parameter. On the contrary, similar values of the pre-posterior and prior variances indicate that monitoring is not expected to bring any significant knowledge improvement.

Let  $p(\theta)$  denote the prior distribution of a generic random variable  $\theta$ , such as a node of the BN which is not deterministic, and  $p(\theta|y)$  the posterior distribution, following an observation  $y$ . The expected value and variance of the posterior distribution of  $\theta$  can be expressed as

$$\mu_{\theta|y}(y) = \frac{\int_{D_\theta} p(\theta|y) \cdot \theta \cdot d\theta}{\int_{D_\theta} p(\theta|y) \cdot d\theta} = \frac{\int_{D_\theta} p(\theta|y) \cdot \theta \cdot d\theta}{p(y)} \quad (5)$$

$$\sigma_{\theta|y}^2(y) = \frac{\int_{D_\theta} p(\theta|y) \cdot (\theta - \mu_{\theta|y}(y))^2 \cdot d\theta}{p(y)} \quad (6)$$

Since the observation is unknown *a priori*, these quantities can be seen as function of the observation  $y$ . The pre-posterior variance can be obtained by taking the expectation with respect to  $y$

$$\begin{aligned} \sigma_{\theta,PP}^2 &= E[\sigma_{\theta|y}^2(y)] = \int_{D_y} \sigma_{\theta|y}^2(y) \cdot p(y) \cdot dy \\ &= \int_{D(\theta,y)} p(\theta|y) \cdot (\theta - \mu_{\theta|y}(y))^2 \cdot d\theta \cdot dy \end{aligned} \quad (7)$$

In practice,  $\sigma_{\theta,PP}^2$  can be estimated with a Monte-Carlo approach. For this purpose, a set of possible monitoring scenarios are generated by performing predictive analysis and generating multiple samples of the possible observations. Each observation is then used as input in a diagnostic analysis to produce a sample of the posterior distribution of the variable of interest. The pre-posterior variance is then obtained by averaging the values of  $\sigma_{\theta|y}^2(y)$  obtained for the different observations.

The expected effectiveness of the monitoring system is measured by the square root of the ratio between the prior and the pre-posterior variances

$$\eta = \sqrt{\frac{\sigma_\theta^2}{\sigma_{\theta,PP}^2}} = \frac{\sigma_\theta}{\sigma_{\theta,PP}} \quad (8)$$

This synthetic parameter can be used to compare the reduction of uncertainty in the estimation of  $\theta$  obtained via alternative monitoring techniques, and can also be used to evaluate the benefits of fusing the data from different sensors. It can be demonstrated that this parameter is always higher than 1, even though for some observations  $y$  the ratio between  $\sigma_\theta^2$  and  $\sigma_{\theta|y}^2(y)$  can be less than 1.

**Reduction of relative entropy.** As an alternative to the pre-posterior analysis approach, a relative entropy measure can be used to quantify the information gain from the available observations. Relative entropy, also called Kullback–Leibler divergence, expresses the difference between two probability distributions when identifying the value of new information or more specifically, observations.<sup>75,76,43</sup> According to Shannon, the information entropy for a random variable  $\theta$  with posterior distribution  $p(\theta|y)$  is defined as the following

$$H[p(\theta|y)] = - \int_{D_\theta} \ln[p(\theta|y)] p(\theta|y) d\theta \quad (9)$$

The cross entropy between two posterior and prior probability distributions, which measures the expected information that is required to get from one distribution to another, is

$$H[p(\theta|y), p(\theta)] = - \int_{D_\theta} \ln[p(\theta)] p(\theta|y) d\theta \quad (10)$$

The relative entropy  $D_{KL}[p(\theta|y), p(\theta)]$  measures the so-called information geometry in moving from the prior to the posterior and can be expressed as

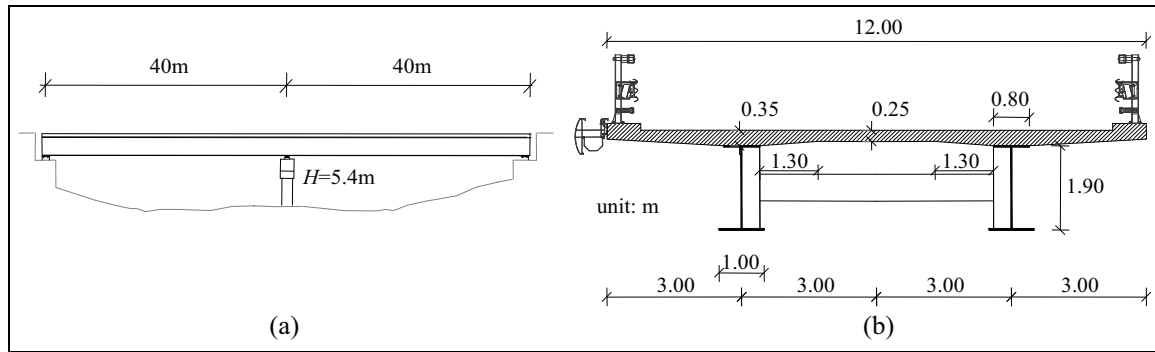
$$\begin{aligned} D_{KL}[p(\theta|y), p(\theta)] &= H[p(\theta|y), p(\theta)] - H[p(\theta|y)] \\ &= \int_{D_\theta} \frac{\ln[p(\theta)]}{\ln[p(\theta|y)]} p(\theta|y) d\theta \end{aligned} \quad (11)$$

According to the formulation, the relative entropy of the observation and reference distribution is lower bounded by 0. In other words, the greater the difference between the two probability distributions, the greater the relative entropy gained from the arrival of observational data. As for the case of the pre-posterior variance, the relative entropy is estimated via a Monte-Carlo approach by averaging all the possible monitoring outcomes. Thus, the obtained effectiveness measure is independent of the specific observation  $y$ .

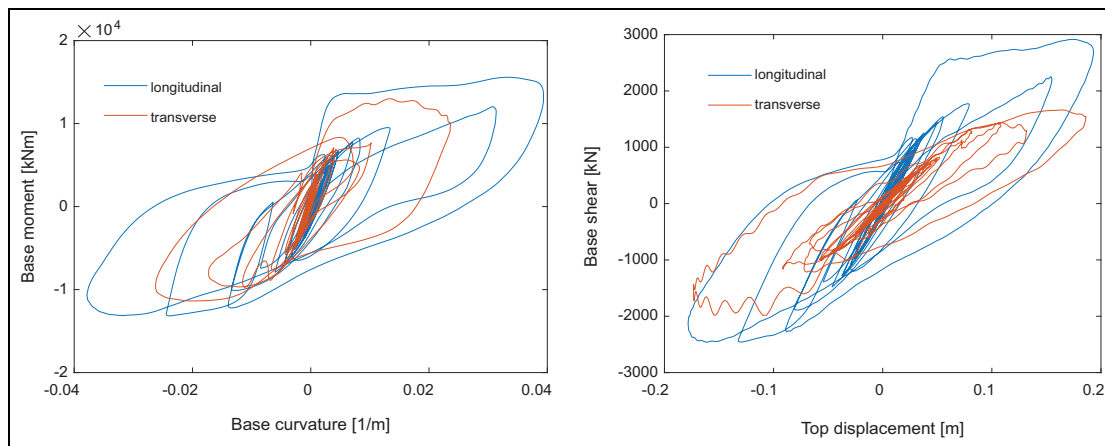
## Case study

In this section, the application of the framework presented above to a bridge structure is described.





**Figure 3.** (a) Two-span bridge profile and (b) transverse deck section.  
Source: Study by Tubaldi et al.<sup>78</sup>



**Figure 4.** (a) Base moment–curvature response and (b) base shear–top displacement response.

### Case study description

**Structural system model for damage and loss assessment.** For demonstration purposes, the structural system considered in this study consists of a two-span bridge with a continuous multi-span steel–concrete composite deck, arbitrarily located in the area of Patras, Greece (longitude 21.906, latitude 38.278, in decimal degrees). The bridge is representative of a class of regular medium-span bridges commonly used in transportation networks<sup>77–78</sup> (see Figure 3). The bridge superstructure, designed according to the specifications given in Eurocode 4,<sup>79</sup> consists of a reinforced concrete slab of width  $B = 12$  m, which hosts two traffic lanes, and of two steel girders positioned symmetrically with respect to the deck centreline at a distance of 6 m. Class C35/45 concrete is used for the superstructure slab. The reinforcement bars are made of grade B450C steel, and the deck girders are made of grade S355 steel. The distributed gravity load due to the self-weight of the deck and of non-structural elements is 138 kN/m, for a weight per unit length  $m_d = 14.07$  ton/m. The reinforced concrete piers have a circular cross-section of

diameter  $D = 1.8$  m. They are made of class C30/37 concrete, with a longitudinal reinforcement steel ratio of 1% and a transverse reinforcement volumetric ratio  $\rho_w = 0.5\%$ . Further details about the bridge can be found in the study by Tubaldi et al.<sup>78</sup>

A three-dimensional finite element (FE) model of the bridge is developed in OpenSees<sup>80</sup> following the same approach described in the study by Tubaldi et al.,<sup>66</sup> that is, using linear elastic beam elements for describing the deck, and the beam element with inelastic hinges developed by Scott and Fennes<sup>81</sup> to describe the pier. Further details of the FE model and of the pier properties are given in the study by Tubaldi et al.<sup>66</sup> The elastic damping properties of the system are described by a Rayleigh damping model, assigning a 2% damping ratio at the first two vibration modes. The FE model described in this study is assumed to be deterministic and characterized by no epistemic uncertainties. Future extensions of the methodology will consider how introducing some uncertainty in the model (e.g. considering the approach outlined by Tubaldi et al.<sup>67</sup>) would affect the results.

Figure 4 shows the hysteretic response of the pier to a bi-directional ground-motion record, in terms of

moment–curvature of the base section, and base shear–top displacement, along the two principal directions of the bridge. It can be observed that the model is characterized by some degradation of stiffness and pinching, that results from the constitutive model adopted to describe the concrete fibres in the plastic hinge region (Concrete 02 in OpenSees<sup>80</sup>). A more sophisticated description of the hysteretic behaviour of the pier is out of the scope of this study.

A set of 221 ground-motion records is used to derive the PSDM: 120 of these were selected by Baker et al.<sup>82</sup> for the performance assessment of a variety of structural systems located in active seismic regions. These records are representative of a wide range of variation in terms of source-to-site distance ( $R$ ) (from 8.71 to 126.9 km), soil characteristics (the average shear wave velocity  $V_S$  in the top 30 m of soil spans from 203 to 2016 m/s) and moment magnitude ( $M_w$ ) (from 5.3 to 7.9), so as to obtain more robust and general results. It is noted that the  $V_S$  values of many of these records are higher than those assumed for deriving the seismic shaking scenarios considered here. This approach, potentially resulting in some bias in the estimation of the PSDM, is consistent with current practice. An alternative approach would have been to select records based on the actual soil conditions at the bridge site and on the actual seismotectonic context around the site. It would have been difficult to find sufficient records to build an accurate PSDM if this approach had been followed. The remaining ground motions are taken from the recordings of different stations during the 1994 Northridge earthquake and they were added to achieve a more confident estimate of the response for high  $IM$  values. The large number of records in the set allows estimation with good confidence of the statistics of the response parameters, even of those which are characterized by a significant dispersion such as the  $RD$ .<sup>48</sup> The median horizontal (geometrical mean) spectral displacement response  $S_d(T)$  at the fundamental period of the bridge ( $T = 0.45$  s) for a damping ratio of 2% is selected as the  $IM$ . It is noteworthy that the GMPE by Akkar and Bommer,<sup>83</sup> which is used in this study, is formulated in terms of the pseudo-spectral acceleration  $S_a(T)$ , which is related to  $S_d(T)$  through the expression  $S_d(T) = S_a(T)/\omega^2$ , where  $\omega = 2\pi/T$ . An amplification factor = 1.195 is used to account for a 2% damping factor instead of 5%, based on the expression for the damping reduction factor taken from Eurocode 8.<sup>82</sup>

The PSDM described in the section ‘Structural analysis’ is fitted to the 221 samples of the various response parameters of interest for the performance assessment, namely the  $RD$  ( $EDP_1 = RD$ ), the  $TD$  ( $EDP_2 = TD$ ) and the  $PA$  ( $EDP_3 = PA$ ). Figure 5 shows the sample values of the  $EDPs$  versus  $IM$  in the log–log plane and

in the untransformed plane. In the same figures, the lognormal mean and median of the fitted PSDM are also plotted. The same value of  $IM^*$  is used for various  $EDPs$ . It is obtained by considering the samples of the  $RDs$ , since the change of slope is more evident from these. In fact, for  $IM \leq IM^*$  the response of the system is in the linear range, and the  $RDs$  are zero, whereas for  $IM > IM^*$  the  $RDs$  assume values different from zero and increase for increasing  $IM$  levels. It is noteworthy that the value of  $IM^* = 0.0286$  m corresponds on average to a drift ratio of 0.68% (defined as the ratio between the  $TD$  and the pier height), which signals the onset of nonlinearity of the system due to concrete cracking and rebar yielding. The peak top displacements and the absolute accelerations increase almost linearly with the seismic intensity and their trend of variation does not change significantly when  $IM$  exceeds  $IM^*$ .

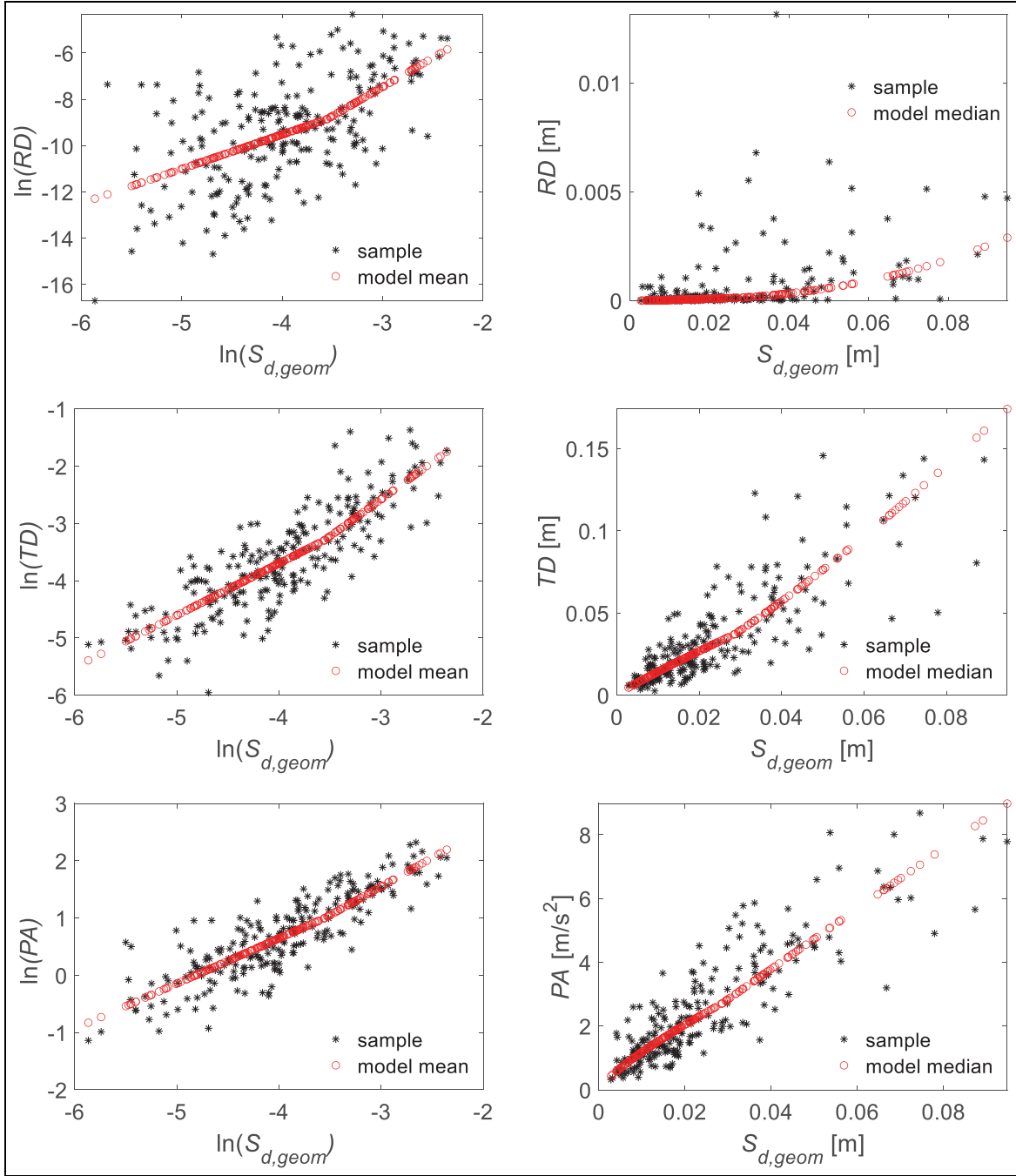
The covariance matrices  $\sum_{EDP}^I$  and  $\sum_{EDP}^{II}$ , collecting the information on the variance of the error variables (in the lognormal space) and on their correlation, for the two branches of the PSDM (corresponding, respectively, to  $IM_1 \leq IM^*$  and  $IM_1 > IM^*$ ) are

$$\begin{aligned} \sum_{EDP}^I &= \begin{bmatrix} 3.700 & 0.271 & 0.039 \\ 0.270 & 0.222 & 0.114 \\ 0.039 & 0.114 & 0.156 \end{bmatrix} \\ \sum_{EDP}^{II} &= \begin{bmatrix} 2.875 & 0.612 & 0.203 \\ 0.612 & 0.293 & 0.126 \\ 0.203 & 0.126 & 0.098 \end{bmatrix} \end{aligned} \quad (12)$$

and the corresponding correlation matrices are

$$\begin{aligned} \mathbf{C}_{EDP}^I &= \begin{bmatrix} 1 & 0.299 & 0.0516 \\ 0.299 & 1 & 0.611 \\ 0.051 & 0.611 & 1 \end{bmatrix} \\ \mathbf{C}_{EDP}^{II} &= \begin{bmatrix} 1 & 0.667 & 0.382 \\ 0.667 & 1 & 0.744 \\ 0.382 & 0.744 & 1 \end{bmatrix} \end{aligned} \quad (13)$$

It can be observed that the  $RDs$  are characterized by significant dispersion, which is much higher than that of the other  $EDPs$ . Moreover, the correlation between the error variable in the PSDM of  $RD$  and the error variable in the PSDMs for the other  $EDPs$  is quite low for  $IM_1 \leq IM^*$ , but it increases for  $IM_1 > IM^*$ . This is expected, since for  $IM_1 \leq IM^*$  the residual drifts are very low. The highest correlations are observed for high seismic intensities between the errors for the PSDMs of  $RD$  and  $TD$  (correlation coefficient of 0.667 for the second branch of the PSDM) and for the PSDMs of  $TD$  and  $PA$  (correlation coefficient of 0.774). The correlation between  $RD$  and  $PA$  is quite low, though not negligible for high seismic intensities (correlation coefficient



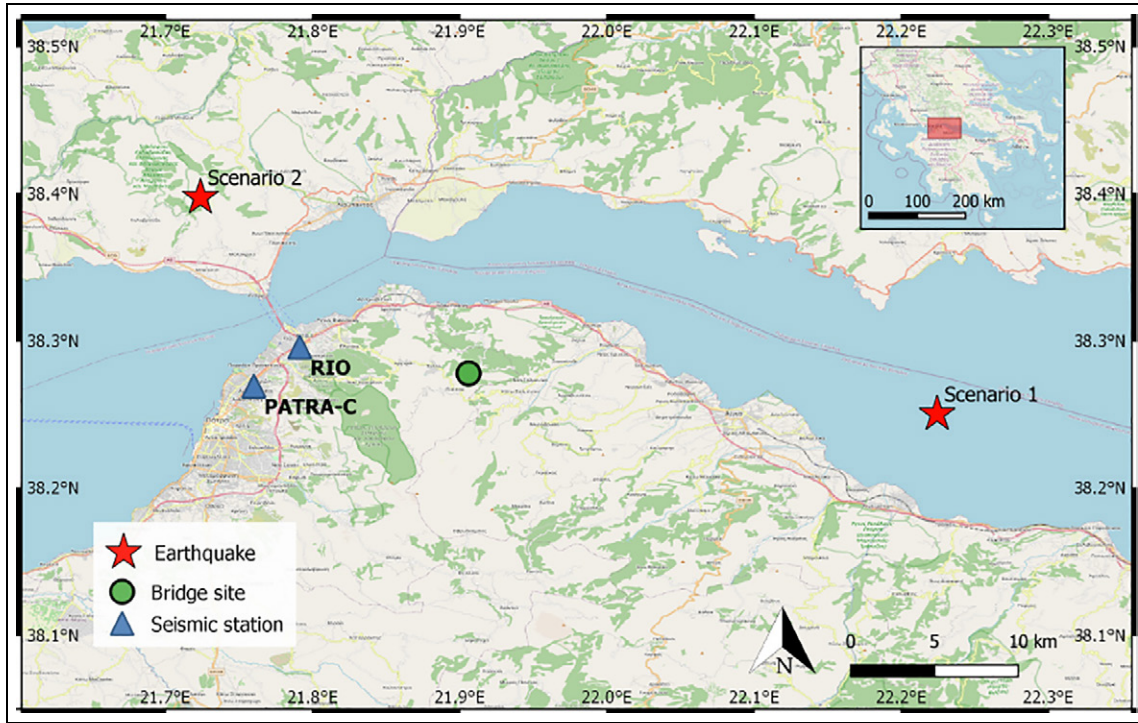
**Figure 5.** Sample values and model results in terms of *RD*, *TD* and *PA* versus *IM* in the log–log plane (left column) and in the untransformed plane (right column).

of 0.382). This suggests that the information on accelerations may be used to reduce uncertainty in the estimation of the bridge’s *TDs* and *RDs*. It is noteworthy that the proposed approach is different from resorting to double integration of the measured acceleration signal for estimating the displacements, which is characterized by several limitations.<sup>85</sup>

The damage of the bridge is assumed to be controlled by the pier. Similar to the study by Choi et al.,<sup>69</sup>

the pier damage is expressed as a function of the ductility demand as follows

$$DS = \begin{cases} \mu < 1 & (\text{no damage}) \\ 1 < \mu < 2 & (DS1) \\ 2 < \mu < 4 & (DS2) \\ 4 < \mu < 7 & (DS3) \\ 7 < \mu & (\text{collapse}) \end{cases} \quad (14)$$



**Figure 6.** Map with indications of bridge site, seismic point sources for scenarios 1 and 2, and seismic stations.

where  $\mu$  and  $DS$  denote, respectively, the ductility demand and the damage state of the bridge. The relationship between the pier top displacement  $TD$  and the ductility demand  $\mu$  is evaluated by performing pushover analysis of the bridge in the longitudinal direction.

The losses are obtained using the equation below<sup>71,72</sup>

$$Loss = \begin{cases} 3\% & (x < DS1) \\ 8\% & (DS1 < x < DS2) \\ 25\% & (DS2 < x < DS3) \\ 100\% & (DS3 < x) \end{cases} \quad (15)$$

**Seismic scenarios and field observations.** It is assumed that the bridge is equipped with one accelerometer and one GPS antenna, both mounted at the level of the superstructure above the pier. The measurement error of the GPS antenna is characterized by a normal distribution with zero mean and a standard deviation of 1 mm, whereas that of the accelerometer is characterized by a normal distribution with zero mean and a standard deviation of  $0.002 \text{ m/s}^2$ . These values are based on the noise root mean square (RMS) levels of exemplary low-cost sensor specifications extracted from representative datasheets (refer to<sup>86</sup> for the noise of a global navigation satellite system (GNSS)-based displacement measurement device and STMicroelectronics<sup>87</sup> for a low-cost micro electro-mechanical systems (MEMS)

accelerometer). The hypothetical bridge is located close to two existing seismic stations (see Figure 6). The first one (PATRA-C) is at the latitude 38.269 and longitude 21.760, whereas the second one (RIO) is at the latitude 38.296 and longitude 21.791. These coordinates correspond to a distance between the site and PATRA-C of 12.8 km, and between the site and RIO of 10.2 km. The distance between the two stations is 4 km.

The seismic hazard at the site is quantified by considering the seismic source zonation of the European Seismic Hazard Model 2013.<sup>88</sup> The earthquake scenarios used in the subsequent sections are two possible realizations obtained by sampling from this model. The prediction of the ground motions at the site from the considered earthquake point sources is made using GMPE by Akkar and Bommer,<sup>83</sup> assuming soft soil conditions ( $V_s < 360 \text{ m/s}$ ) and a strike-slip fault mechanism. The spatial correlation model proposed by Jayaram and Baker<sup>47</sup> is used to build the correlation matrix  $\mathbf{C}_{IM}$  expressing the correlation between the  $IMs$  at different sites. The terms of  $\mathbf{C}_{IM}$  are the correlation coefficients  $\rho_{ij}$  between the ground-motion parameters at two sites  $i$  and  $j$ , expressed as

$$\rho_{ij} = \exp\left(-\frac{3r_{ij}}{b}\right) \quad (16)$$

in which  $r_{ij}$  is the distance between the sites and  $b$  is the correlation distance.

It is noteworthy that the correlation distance varies significantly from site to site and from earthquake to earthquake, and it also changes with the structural period.<sup>46</sup> Equations for capturing the dependence of  $b$  on these parameters are provided by Jayaram and Baker,<sup>47</sup> from which the value of  $b$  for this study (15.9 km) is taken.

As a result, the covariance matrix  $\Sigma_{\text{IM}}$  related to the IMs ( $IM_1$ ,  $IM_2$ ,  $IM_3$  corresponding, respectively, to the bridge site, and the PATRA-C and RIO stations) in lognormal space, as well as the spatial correlation matrix  $C_{\text{IM}}$  between the sites, are estimated as follows

$$\begin{aligned} \Sigma_{\text{IM}} &= \begin{bmatrix} 0.105 & 0.021 & 0.026 \\ 0.021 & 0.105 & 0.056 \\ 0.026 & 0.056 & 0.105 \end{bmatrix} \\ C_{\text{IM}} &= \begin{bmatrix} 1 & 0.089 & 0.146 \\ 0.089 & 1 & 0.470 \\ 0.146 & 0.470 & 1 \end{bmatrix} \end{aligned} \quad (17)$$

It is worth noting that the correlation values between the sites are very low, which is due to the quickly decreasing spatial correlation model. However, the arbitrary case study that is defined here is consistent with the usual seismic network density in Europe (e.g. exposed sites are often a dozen kilometres or more away from the nearest seismic station). Since the information gain provided by the seismic stations in terms of uncertainty reduction at the bridge site is expected to be low due to the low correlation between  $IM_1$  and  $IM_2$  and  $IM_3$ , the case of a ground accelerometer placed at the base of the bridge is also considered to quantify the maximum uncertainty reduction achievable by a perfect knowledge of the  $IM_1$ .

### Rapid damage assessment for a single scenario

This subsection describes the results of the Bayesian updating for scenario 1, which corresponds to the seismic point source 1, with Magnitude  $M_w$  5, located 28.0 km from the site and 40.6 and 38.2 km from the stations PATRA-C and RIO, respectively (Figure 6).

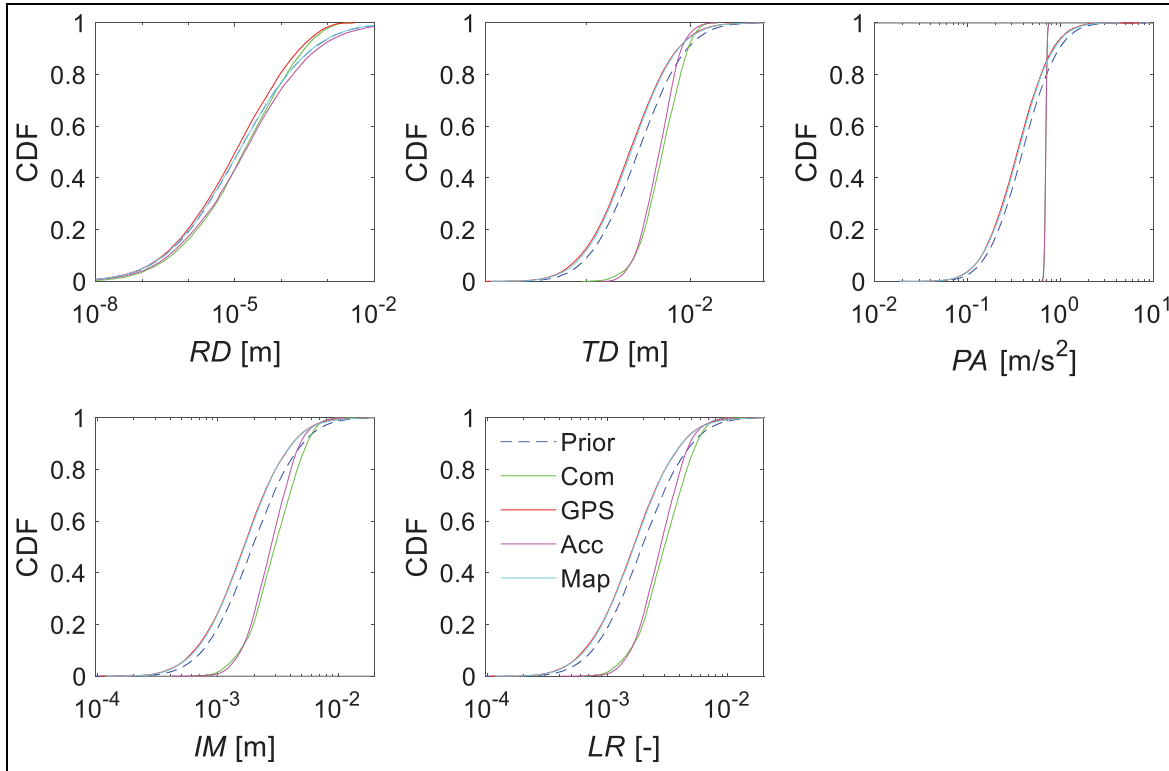
Predictive analysis is first run based on the information at the root nodes (including the deterministic ones,  $M_w$  and  $\mathbf{R}_e$ , that describe the earthquake scenario). Subsequently, multiple independent diagnostic analyses are performed by entering a piece of evidence one at a time at the nodes  $IM_2$ ,  $IM_3$ ,  $RD_{\text{obs}}$  and  $PA_{\text{obs}}$  and also by entering all the information at these nodes at the same time. These analyses are performed with OpenBugs<sup>74</sup> using three MCMC chains generated with different combinations of initial conditions. This is to ensure that the three different starting points converge towards similar posterior distributions. Each chain

contains 10,000 samples, which are obtained by starting from 60,000 iterations, discarding the first 10,000 (burn-in) and thinning to reduce autocorrelation. Ultimately, a total of 30,000 samples is used to estimate the posterior distributions. It is noteworthy that the time required to perform a single Bayesian Inference analysis is quite low (of the order of a few seconds on a standard personal computer).

Figure 7 shows the empirical cumulative distribution function (CDF) for the prior distribution of the various parameters of interest, and the posterior distributions given the observations of the GPS, accelerometers (Acc) and seismic stations (Map). The results obtained by combining the observations are also shown for comparison (Com). Table 2 reports median values and standard deviations of the prior and posterior distributions, together with the observations from the various sensors.

The prior distribution is characterized by low values of the various *EDPs*, as expected, given the low magnitude and high epicentral distance of the source. Thus, the expected losses are zero. The *RDs* are very small, though significantly dispersed, with a value of lognormal standard deviation  $\beta$  of the order of 2.8, whereas the other parameters are characterized by smaller dispersion, with values of  $\beta$  of the order of 0.7–0.8. The information from the sensors generally results in a reduction of the uncertainty, corresponding to a steeper empirical CDF for the posterior distributions of the parameters of interest compared to the prior, and to a reduced lognormal standard deviation. The use of an accelerometer clearly outperforms the other sensing strategies in terms of uncertainty reduction. In particular, using the accelerometer, the dispersion of the absolute acceleration of the deck reduces from 0.7 to about 0.03, but the dispersion of the *RDs* remains unvaried, due to the low correlation between accelerations and *RDs* for low seismic intensities, when the *RDs* are very low. The reduction of uncertainty of the *RDs* is not significant even if GPS data are used, due to the significant noise-to-signal ratio, thus resulting in a reduction in the dispersion of the residual only by 10%. The overall reduction of uncertainty is more significant if the combined observations from the various sensors are used. However, there is only a minimal improvement by considering additional information from other sensors if the accelerometers are already used, as demonstrated by the fact that the distributions of all the *EDPs*, with the exception of the *RD* for the Acc and Com cases, almost overlap.

A larger earthquake (scenario 2) is considered, which corresponds to a realization generated considering seismic point source 2, with magnitude  $M_w$  6.5, located 20.7 km from the site and 14.6 and 12.7 km from the stations PATRA-C and RIO, respectively (Figure 6).



**Figure 7.** Empirical cumulative distribution function (CDF) of the parameters of interest before and after updating with observations from scenario I.

**Table 2.** Median and lognormal standard deviation of prior and posterior distribution of parameters of interest for a realization from scenario I.

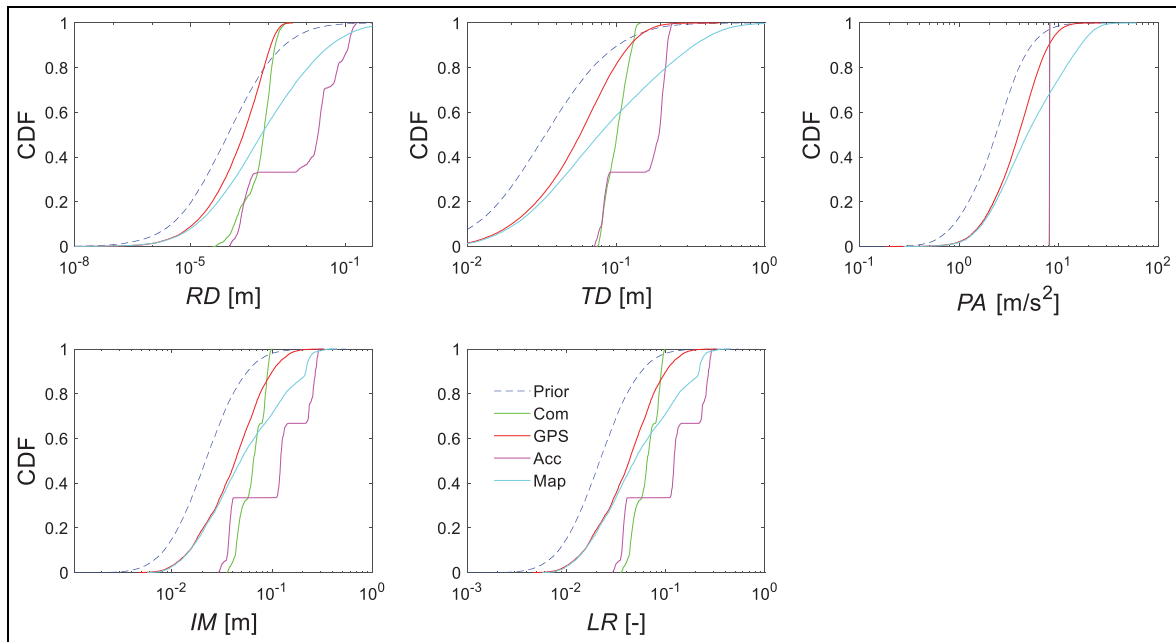
Observation source	Observation	RD		TD		PA		IM		LR	
		Median (m)	$\beta$	Median (m)	$\beta$	Median (m/s <sup>2</sup> )	$\beta$	Median (m)	$\beta$	Median (-)	$\beta$
None (prior)	–	$1.22 \times 10^{-5}$	2.873	0.0031	0.845	0.389	0.704	0.0019	0.744	0	0
Seismic stations	0.0011 m, 0.0000596 m	$1.20 \times 10^{-5}$	2.877	0.00270	0.828	0.351	0.696	0.0017	0.724	0	0
GPS	$2.8 \times 10^{-4}$ m	$1.02 \times 10^{-5}$	2.599	0.00260	0.834	0.343	0.691	0.0016	0.726	0	0
Accelerometer	0.672 m/s <sup>2</sup>	$1.60 \times 10^{-5}$	2.897	0.00449	0.406	0.695	0.029	0.0028	0.447	0	0
Combined	–	$1.45 \times 10^{-5}$	2.491	0.005	0.446	0.694	0.029	0.0028	0.486	0	0

RD: residual displacement; TD: peak transient displacement; PA: peak absolute acceleration; IM: intensity measure; LR: loss ratio; GPS: global positioning system.

The results corresponding to this realization are shown in Figure 8 and in Table 3.

In this case, the prior distribution is characterized by relatively high values of the *TD*, resulting in a median drift ratio of 0.78%, which corresponds to an inelastic behaviour of the pier. However, the median value of the *RD* is still very low, as a result of the hysteretic behaviour of the pier and the stiffness degradation and pinching (see Figure 4). The realization considered is

characterized by a high value of the observation of the accelerometer compared to the prior median estimate, which results in an increased median value of *PA* and of the other response parameters compared to the prior one. It is noteworthy that the posterior CDFs of all the monitored random variables (with the exception of the absolute accelerations) updated considering the observation of the accelerometer are characteristic of a bimodal distribution. This can again be explained by the



**Figure 8.** Empirical cumulative distribution function (CDF) of the parameters of interest before and after updating with observations from scenario 2.

observation that the  $PA$  is significantly different from the median value of the prior (three times higher), which is also the result of the relatively high noise-to-signal ratio of the accelerometer. It is also worth observing that there is also an increase in the dispersion of all the parameters that are not directly measured by the accelerometers. The median value of the  $LR$  increases from 0 to 1, although the dispersion increases too. Using the information from ShakeMaps also results in a general increase of median values and of dispersion of the parameters. This is because the observed values of  $IM_2$  and  $IM_3$  (0.0627 and 0.0904 m, respectively) are higher than the median values of the prior estimates (0.0429 and 0.0488 m, respectively). The GPS observations do not change the median values significantly but reduce the dispersions slightly. Combining the observations from the various sensors results in lower uncertainty in the estimates of the  $RD$ ,  $TD$ ,  $PA$  and  $IM$  compared to the prior estimates, whereas the uncertainty in the  $LR$  remains quite high. This trend may be explained by the fact that all the observed quantities (i.e.  $IM$ s at seismic stations,  $RD$ s and  $PA$ s of the bridge) are consistently higher than the median prior estimates and thus when the observations are combined, this results in more confident and less-disperse estimates of the EDPs. It is noteworthy that in order to properly quantify the uncertainty reduction, the average results from multiple realizations of observations must be considered, as discussed in the section ‘Quantification of

sensors’ effectiveness for uncertainty reduction’ and done in the subsequent subsection.

### Quantification of uncertainty reduction

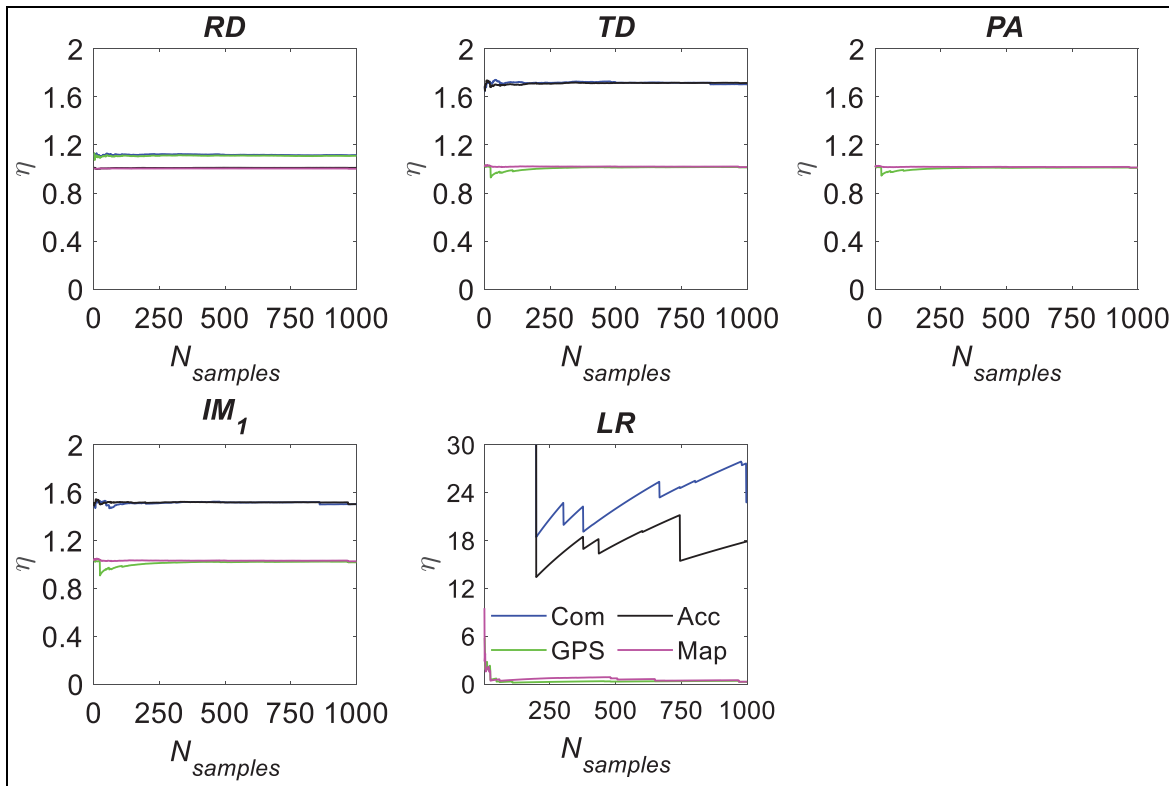
This subsection describes the results of the quantification of the uncertainty reduction for the two earthquake scenarios of Figure 6. In particular, Figure 9 illustrates the evolution of the estimates of  $\eta$  for the various parameters of interest with the number of samples drawn from scenario 1 (moderate earthquake). The results for  $PA$  when accelerometer observations are used are not shown because they are very high due to the low noise-to-signal ratio. It can be observed that 1000 samples are sufficient to achieve quite accurate estimates of this monitoring effectiveness measure based on pre-posterior variance analysis for all the parameters of interest. For the case of the loss ratio  $LR$ , characterized by higher values of  $\eta$  and a lower convergence rate, 2000 samples are required. Considering more samples would not significantly increase the accuracy of the estimates. With this number of samples, confident estimates of the values of the relative entropy measure  $D_{KL}$  can also be achieved for all the parameters of interest.

Tables 4 and 5 show the values of the effectiveness measures obtained based on the pre-posterior variance and the reduction of relative entropy for scenarios 1 and 2, respectively. These estimates of  $\eta$  and  $D_{KL}$  are

**Table 3.** Median and lognormal standard deviation of prior and posterior distribution of parameters of interest for a realization from scenario 2.

Observation source	Observation	RD		TD		PA		IM		LR	
		Median (m)	$\beta$	Median (m)	$\beta$	Median (m/s <sup>2</sup> )	$\beta$	Median (m)	$\beta$	Median (-)	$\beta$
None (prior)	–	$9.2 \times 10^{-5}$	2.672	0.042	0.857	2.76	0.696	0.0272	0.744	0	0.04
Seismic stations	0.0627 m, 0.0904 m	$6.67 \times 10^{-4}$	3.0744	0.077	1.040	4.826	0.855	0.0486	0.947	0.08	0.5
GPS	$5.4 \times 10^{-4}$ m	0.00023	1.841	0.057	0.702	3.955	0.607	0.0429	0.719	0.03	0.125
Accelerometer	8.103 m/s <sup>2</sup>	0.0195	2.52	0.194	0.437	8.1	0.002	0.122	0.807	1	1.097
Combined	–	0.0008	0.919	0.101	0.172	8.1	0.002	0.065	0.282	0.25	1.339

RD: residual displacement; TD: peak transient displacement; PA: peak absolute acceleration; IM: intensity measure; LR: loss ratio; GPS: global positioning system.

**Figure 9.** Evolution with the number of samples of the monitoring effectiveness measure based on pre-posterior variance for the various parameters of interest and observation sources (scenario 1).

based on 1000 samples in the case of all the parameters except *LR*, for which 2000 samples are used. With regard to the first measure of effectiveness, it can be observed that the values of  $\eta$  are all higher than 1 as expected, since adding information from sensors can only reduce uncertainty on average. For the same reason, the combined observations from multiple sensors result in a higher effectiveness, due to the lower variance of the parameters of interest compared to that obtained with a single sensor's observation. GPSs are

the most effective sensors for reducing the uncertainty in the residual drifts, and their effectiveness increases with the seismic intensity, since for low intensities the noise-to-signal ratio of the *RD* is high (the *RD*s are zero until the pier yields). Accelerometers are the most effective sensors for reducing the uncertainty of the *PA*, and also of the *TD*, given the significant correlation existing between *PA* and *TD*. The information from seismic stations located at reasonable distance from the site does not provide any benefit in terms of



**Table 4.** Pre-posterior variance-based effectiveness measure for estimation of various parameters of interest.

Scenario	$M_w$ (-)	$R$ (km)	Observation source	$RD$	$TD$	$PA$	$IM$	$LR$
1	5	30	Seismic stations (1)	1.002	1.015	1.011	1.025	1.000
			GPS (2)	1.110	1.012	1.000	1.017	1.000
			Accelerometer (3)	1.010	1.717	9.315	1.504	15.150
			Ground accelerometer (4)	1.003	1.982	1.507	28.020	4.575
			Combined (1,2,3)	1.120	1.730	9.327	1.524	15.150
2	6.5	20.7	Combined (2,3,4)	1.124	2.321	10.009	28.280	42.580
			Seismic stations (1)	1.000	1.000	1.000	1.000	1.000
			GPS (2)	1.344	1.055	1.008	1.017	1.086
			Accelerometer (3)	1.000	1.477	49.220	1.000	1.921
			Ground accelerometer (4)	1.277	1.869	2.164	316.160	1.305
			Combined (1,2,3)	1.428	2.305	49.220	1.026	2.348
			Combined (2,3,4)	1.579	3.531	50.430	317.826	2.250

$RD$ : residual displacement;  $TD$ : peak transient displacement;  $PA$ : peak absolute acceleration;  $IM$ : intensity measure;  $LR$ : loss ratio; GPS: global positioning system.

**Table 5.** Reduction of relative entropy-based effectiveness measure for estimation of various parameters of interest.

Scenario	$M_w$ (-)	$R$ (km)	Observation source	$RD$	$TD$	$PA$	$IM$	$LR$
1	5	30	Seismic station (1)	0.045	0.193	0.164	0.472	0.012
			GPS (2)	9.004	0.195	0.152	0.323	0.017
			Accelerometer (3)	0.121	28.261	182.464	18.838	0.200
			Ground accelerometer (4)	0.094	31.891	11.628	211.279	0.176
			Combined (1,2,3)	9.729	28.625	182.279	18.960	0.201
2	6.5	20.7	Combined (2,3,4)	11.403	58.142	184.095	211.551	0.200
			Seismic station (1)	0.374	1.217	1.259	5.415	0.073
			GPS (2)	31.771	8.794	6.296	12.151	0.139
			Accelerometer (3)	31.983	72.592	215.994	111.206	34.637
			Ground accelerometer (4)	4.126	27.991	41.805	220.421	4.067
			Combined (1,2,3)	51.566	119.331	216.049	112.024	36.688
			Combined (2,3,4)	62.447	132.049	214.224	220.441	32.072

$RD$ : residual displacement;  $TD$ : peak transient displacement;  $PA$ : peak absolute acceleration;  $IM$ : intensity measure;  $LR$ : loss ratio; GPS: global positioning system.

uncertainty reduction, given the low correlation existing between the  $IM$  at the site and that at the stations.

The reduction of uncertainty achieved for the losses is high in the case of low seismic intensity, and low for high seismic intensity. Moreover, in the case of low levels of shaking, sensors mounted on a structure can help to reduce the uncertainty in the estimation of the shaking intensity, and thus can be used to further improve ShakeMaps and achieve better estimates of the losses at structures not directly equipped with sensors. In the case of strong earthquakes, this effect of uncertainty reduction in the estimation of the  $IM$  is lost.

To shed further light on the reduction of uncertainty achievable with information on ground-shaking intensity, the case of a ground accelerometer placed at the base of the structure is also considered, providing an upper bound of the benefit in terms of uncertainty reduction derived from the use of ShakeMaps. It can be observed that if the seismic stations are located very

close to the site, then the information they provide helps to reduce the uncertainty of the various parameters of interest. Similar observations were made in other studies,<sup>89,90</sup> indicating that a very dense network of seismometers in the vicinity of the site is required to obtain accurate estimates of the ground-motion intensity.

With regard to the second measure of the sensors' effectiveness ( $D_{KL}$ ), the observed trends are quite similar to those obtained for the first one, that is, the accelerometer mounted on the structure is the most effective for estimating displacements and accelerations, the GPS for the residuals, and higher effectiveness is achieved by combining more and more data. The reduction of uncertainty associated with ShakeMaps observations is quite low but slightly higher in the case of higher seismic intensities. This phenomenon is again explained by the distance from the two seismic stations to the bridge site (i.e. around a dozen kilometres), which is close to the spatial correlation distance of the

Jayaram and Baker<sup>47</sup> model, that is, 15.9 km. As a result, the updates made to the values of the *IM* are much reduced, highlighting the need to deploy dense networks of seismic stations around exposed assets.

The only significant difference between the trends of the two effectiveness measures is for the *LR* estimates for scenario 1, characterized by high values of  $\eta$  for the accelerometer and combined observations, and generally low values of  $D_{KL}$  for all the observations. The opposite trend is observed for scenario 2. This discrepancy can be caused by the fact that the losses are generally very small, with a median value of 0 of the prior distribution. Moreover, in contrast to what is observed using the other effectiveness measurement, the reduction of uncertainty in the *IM* due to the observations is quite significant.

## Conclusion and future work

This article illustrates a Bayesian framework for near real-time seismic damage assessment of critical structures that exploits heterogeneous sources of information from ShakeMaps, GPS receivers and accelerometers placed on the structure. Two alternative measures are proposed for quantifying the reduction of uncertainty from the observations, based on the concepts of pre-posterior variance and relative entropy reduction. The proposed framework is applied to investigate the effectiveness of the alternative sensing strategies for the rapid estimation of the response and the losses at a bridge under a moderate and a strong earthquake scenario.

Based on the observed results, the following conclusions can be drawn:

- Among the sensors considered, the GPS sensor provides the best results in terms of uncertainty reduction when used to compute *RDs* of the piers, whereas the accelerometer placed at the top of the deck provides the best results in terms of reducing the uncertainty in the estimate of the absolute accelerations and drifts. The expected effectiveness of ShakeMaps is quite low, unless a seismic station is located very close to the structure.
- The effectiveness of the sensors changes significantly with the shaking intensity. In the case of low shaking intensity, the effectiveness of the sensors in reducing the uncertainty is jeopardized by noise/measurement errors, particularly in the case of *RDs*. These errors become less significant in the case of high seismic shaking.
- When the data from different sensors are combined together through the proposed BN, higher

reductions of uncertainty are achieved as compared to when only single observation sources are considered separately.

- The reduction of uncertainty in the losses can be very significant, whereas that in the estimate of the seismic shaking intensity is generally quite low.
- The two measures of the monitoring effectiveness provide consistent results for most of the observed parameters and can be used interchangeably to quantify the reduction of uncertainty achievable with a monitoring strategy.

Future studies will address the quantification of the effectiveness of earthquake early warning techniques with a similar approach to that developed in this study and will also address alternative structural health monitoring schemes. Moreover, the proposed framework and results of these analyses will be used to develop a decision support system for bridges under extreme scenarios and to define optimal actions based on expected utility theory concepts. While the present study has demonstrated theoretical concepts on an arbitrary case study, further efforts within the TURNkey project (<http://www.earthquake-turnkey.eu>) may lead to an actual test and implementation of the approach, including the collection of real measurements.

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