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Shoreline instability under low-angle wave incidence

D. Idier

- ² BRGM, 3 Avenue C. Guillemin, BP 6009, 45060 Orléans Cedex 2, France
 - A. Falqués
- ³ UPC, C/ Jordi Girona 1-3, Modul B4/B5, despatx 103 E-08034, Barcelona,
- 4 Catalonia, Spain
 - B.G. Ruessink
- 5 Utrecht University, Institute for Marine and Atmospheric Research Utrecht,
- ⁶ Faculty of Geosciences, Department of Physical Geography, P.O. box 80115,
- ₇ 3508 TC Utrecht, The Netherlands
 - R. Garnier
- Instituto de Hidráulica Ambiental IH Cantabria, Universidad de Cantabria,
- ETSI Caminos Canales y Puertos, Avda. los Castros s/n, 39005 Santander,
- 10 Cantabria, Spain

- D. Idier, BRGM, 3 Avenue C. Guillemin, BP 6009, 45060 Orléans Cedex 2, France. (d.idier@brgm.fr)
- A. Falqués, UPC, C/ Jordi Girona 1-3, Modul B4/B5, despatx 103 E-08034, Barcelona, Catalonia, Spain. (falques@fa.upc.edu)

11 Abstract.

- The growth of megacusps as shoreline instabilities is investigated by examining the coupling between wave transformation in the shoaling zone, long-13 shore transport in the surf zone, cross-shore transport, and morphological evolution. This coupling is known to drive a potential positive feedback in case of very oblique wave incidence, leading to an unstable shoreline and the consequent formation of shoreline sandwaves. Here, using a linear stability model based on the one-line concept, we demonstrate that such instabilities 18 can also develop in case of low-angle or shore-normal incidence, under certain conditions (small enough wave height and/or large enough beach slope). The wavelength and growth time scales are much smaller than those of high-21 angle wave instabilities and are nearly in the range of those of surf zone rhyth-22 mic bars, $O(10^2 - 10^3 \text{ m})$ and O(1 - 10 days), respectively. The feedback 23 mechanism is based on: (1) wave refraction by a shoal (defined as a crossshore extension of the shoreline perturbation) leading to wave convergence 25 shoreward of it, (2) longshore sediment flux convergence between the shoal and the shoreline, resulting in megacusp formation, and (3) cross-shore sed-
 - B.G. Ruessink, Utrecht University, Institute for Marine and Atmospheric Research Utrecht, Faculty of Geosciences, Department of Physical Geography, P.O. box 80115, 3508 TC Utrecht, The Netherlands. (b.g.ruessink@uu.nl)
 - R. Garnier, IH Cantabria, Universidad de Cantabria, Avda. los Castros s/n, 39005 Santander, Cantabria, Spain. (garnierr@unican.es)

- 28 iment flux from the surf to the shoaling zone, feeding the shoal. Even though
- 29 the present model is based on a crude representation of nearshore dynam-
- ics, a comparison of model results with existing 2DH model output and lab-
- oratory experiments suggests that the instability mechanism is plausible. Ad-
- ditional work is required to fully assess whether and under which conditions
- this mechanism exists in nature.

1. Introduction

Rhythmic shorelines featuring planview undulations with a relatively regular spacing or wavelength are quite common on sandy coasts. In the present study, we focus on undulations that are linked to submerged bars or shoals and are generally known as shoreline sandwaves [Komar, 1998; Bruun, 1954]. These sandwaves can be classified according to their length scale as short and long sandwaves (see, e.g., Stewart and Davidson-Arnott [1988]).

The spacing of short sandwayes ranges from several tens to several hundreds of meters 40 and their seaward perturbations are known as megacusps. Observations show that these 41 megacusps can develop shoreward of crescentic bar systems during the typical "Rhythmic Bar and Beach" morphological beach state or can develop from the shore attachment 43 of transverse bars that characterise the "Transverse Bar and Beach" state [Wright and Short, 1984. These transverse bars can appear where the horns of a previous crescentic bar approach the shoreline [Wright and Short, 1984; Sonu, 1973; Ranasinghe et al., 2004; Lafon et al., 2004; Castelle et al., 2007. On the other hand, transverse bars can also develop freely, independently of any offshore rhythmic system (e.g. the "transverse finger bars" [Sonu, 1968, 1973; Ribas and Kroon, 2007]). The formation of rhythmic surf zone bars and associated megacusps is believed to be due primarily to an instability of the 50 coupling between the evolving bathymetry and the distribution of wave breaking (bedsurf coupling) [Falqués et al., 2000]. The developing shoals and channels cause changes in 52 wave breaking, which in turn cause gradients in radiation stresses and thereby horizontal circulation with rip currents. If the sediment fluxes carried by this circulation converge

over the shoals and diverge over the channels, a positive feedback arises and the coupled system self-organizes to produce certain patterns, both morphological and hydrodynamic (see, e.g., Reniers et al. [2004]; Garnier et al. [2008]). In the case of oblique wave incidence, a meandering of the longshore current is also essential to the instability process [Garnier et al., 2006]. Two important characteristics of all available models of the self-organized formation of rhythmic surf zone bars are that they (1) are essentially based on sediment transport driven by the longshore current and rip currents only, i.e. ignore cross-shore transport induced by undertow and wave non-linearity and (2) do not consider morphological changes beyond the offshore reach of the rip-current circulation.

Rhythmic shorelines can also develop as a result of an instability not related to bed-64 surf coupling. Ashton et al. [2001] and Ashton and Murray [2006a, b] have shown that 65 sandy shorelines are unstable for wave angles (angle between wave fronts and the local shoreline orientation) larger than about 42° in deep water, leading to the formation of 67 shoreline sandwaves, cuspate features and spits. Falqués and Calvete [2005] have found that the initial characteristic wavelength of the emerging sandwayes is in the range of 3 to 69 15 km, i.e., much larger than that of surf zone rhythmic bars. This instability caused by high-angle waves will henceforth be referred to as HAWI (High-Angle Wave Instability). 71 The physical mechanism can be explained as follows. For oblique wave incidence, there are essentially two counteracting effects. On one hand, the angle relative to the local 73 shoreline is larger on the lee of a cuspate feature than on the updrift side. This tends to 74 cause larger alongshore sediment flux at the lee and thereby divergence of sediment flux along the bump, which therefore tends to erode. On the other hand, since the refractive wave ray turning is stronger at the lee than at the updrift flank, there is more wave energy

spreading due to crest stretching at the lee causing smaller waves and smaller alongshore sediment flux. This produces convergence of sediment flux at the bump, which therefore tends to grow. For high angle waves the latter effect dominates and, if the bathymetric 80 perturbation associated with the shoreline feature extends far enough offshore, it leads to 81 the development of the cuspate feature. In contrast to the bed-surf instability for rhythmic 82 surf zone bars, this instability mechanism depends essentially on the coupling between the 83 surf and shoaling zones. Indeed, the gradients in alongshore sediment flux that induce bathymetric changes in the surf zone occur because of wave field perturbations induced by 85 bathymetric features in the shoaling zone. Thus, in order to achieve a positive feedback, the shoals (or the bed depressions) in the surf zone must extend into the shoaling zone. 87 This is achieved by the cross-shore sediment fluxes induced, for instance, by wave nonlinearity, gravity and undertow, which force the cross-shore shoreface profile to reach an equilibrium profile. HAWI may provide an explanation for the self-organized formation of some long shoreline sand waves which are reported in the literature [Verhagen, 1989; Inman et al., 1992; Thevenot and Kraus, 1995; Ruessink and Jeuken, 2002; Davidson-92 Arnott and van Heyningen, 2003]. On the other hand, some observations for low incidence angles show that longshore 94 currents can converge on megacusps because of wave refraction [Komar, 1998]. Such current convergence may lead to longshore sediment flux convergence and hence to megacusp growth. If the submerged part of the megacusp grows and extends far enough into the 97 shoaling zone (due to the cross-shore transport leading to an equilibrium profile), wave

refraction would be enhanced and a positive feedback would arise. This might provide a

some similitude with HAWI in the sense that the coupling between the surf and shoaling zones is essential, in contrast to the bed-surf instability. We will refer to this potential mechanism as Low-Angle Wave Instability (LAWI). The aim of the present contribution is to investigate this new morphodynamic instability mechanism and discuss whether the resulting shoreline instability may be found in nature.

The lay-out of this paper is as follows. First (Section 2), we introduce the 1D-morfo model [Falqués and Calvete, 2005] that we used to investigate LAWI. Numerical experiments of idealized cases are presented and analyzed in Section 3. We find that shoreline sandwaves can indeed develop because of LAWI, with a length scale comparable to those of megacusps and rhythmic surf zone bars. In Section 4, we analyze the physics of the instability mechanism. We conclude our paper with a discussion and a summary of the main results.

2. The shoreline stability model: 1D-morfo

Owing to the similar with HAWI [Ashton et al., 2001; Falqués and Calvete, 2005], the 113 LAWI mechanism is assumed to be un-related to surf zone processes like rip or longshore meandering currents. Thus, the engineering simplification of one-line modeling [Dean 115 and Dalrymple, 2002 is used, where the shoreline dynamics are based on alongshore 116 gradients in the total alongshore transport rate, Q (i.e., the total volume of sand carried 117 by the wave-driven longshore current that crosses a cross-section of the surf zone area for unit of time (m^3/s)). Using such a simple model, which neglects numerous aspects 119 of surf zone dynamics, including rip current circulation, longshore current meandering, 120 and thus the bed-surf coupling phenomena, allows to investigate properly whether the 121 LAWI mechanism is supported by the governing equations. Furthermore, the consistency 122

of the sediment transport patterns from the one-line modelling has been confirmed by using a 2DH model (delft3D) [List and Ashton, 2007], at least in case of HAWI. These reasons, in addition to the fact that HAWI has been studied and reproduced with a linear stability model called 1D-morfo based on the one-line concept, lead us to use the same model to investigate LAWI and its differences with HAWI. A very brief description of the 128 1D-morfo model is given here. The reader is referred to Falqués and Calvete [2005] for further details.

The model describes the dynamics of small amplitude perturbations of an otherwise rectilinear coastline. Following the one-line concept, the dynamics are governed by gradients in the total alongshore wave-driven transport rate Q:

$$\bar{D}\frac{\partial x_s}{\partial t} = -\frac{\partial Q}{\partial y} \tag{1}$$

A Cartesian coordinate system is used, with x increasing seaward in the unperturbed 133 cross-shore direction and y running alongshore (Figure 1). The position of the shoreline is given by $x = x_s(y, t)$, where t is time and \bar{D} is the active water depth (as defined by 135 Falqués and Calvete [2005]), which is of the order of the depth of closure. This active 136 water depth is directly related to the one-line model concept, for more details, see Falqués 137 and Calvete [2005]. The transport rate Q is computed according to the longshore sediment 138 transport equation of Ozasa and Brampton [1980]. In this formulation, Q is the sum of two terms: the first one (Q_1) is driven by waves approaching the shore at an angle and 140 is equivalent to the CERC formula [USACE, 1984], and the second one (Q_2) takes into 141 account the influence of wave set-up induced currents related to the alongshore gradient 142 in the wave height.

The equation of the sediment transport rate Q can be written as follows:

$$Q = Q_1 + Q_2 \qquad Q = \mu H_b^{5/2} \left(\sin(2(\theta_b - \phi)) - r \frac{2}{\beta} \cos(\theta_b - \phi) \frac{\partial H_b}{\partial y} \right)$$
(2)

where H_b is the (rms) wave height at breaking (index b), θ_b is the angle between wave fronts and the unperturbed coastline at breaking, and $\phi = \tan^{-1}(\partial x_s/\partial y)$ is the local orientation of the perturbed shoreline. β is the beach slope at the instantaneous shoreline 147 (i.e. the waterline). The constant μ is proportional to the empirical parameter K_1 of the original CERC formula and is $\sim 0.1 - 0.2 \text{ m}^{1/2} \text{s}^{-1}$. For the reference case of this 149 paper, a value, $\mu = 0.15 \text{ m}^{1/2} \text{s}^{-1}$, was chosen, which corresponds to $K_1 = 0.525$. The nondimensional parameter r is equal to K_2/K_1 , where K_2 is the empirical parameter of 151 Ozasa and Brampton [1980]. According to Horikawa [1988], r ranges between 0.5 and 1.5, 152 whereas Ozasa and Brampton [1980] suggest a value of 1.62. The value r=1 is used for 153 the present reference case, which is equivalent to $K_2 = K_1$ and has been used in several 154 earlier studies on shoreline instabilities [Bender and Dean, 2004; List et al., 2008; van den Berg et al., 2011]. However, the term Q_2 is not always taken into account, and its validity 156 and application range are uncertain. In section 3.2, we will study the sensitivity of our 157 results to the value of r. 158

Some discussion exists about the capacity of the CERC formula (Q_1) to predict correctly gradients in alongshore sediment transport in the presence of bathymetric perturbations [List et al., 2006, 2008; van den Berg et al., 2011]. The results of List and Ashton [2007] suggest that the CERC formula predicts qualitatively correct transport gradients for large scale shoreline undulations (alongshore lengths of 1-8 km). The term Q_2 was introduced to describe the sediment transport resulting from alongshore variations in the breaker wave height induced by diffraction near coastal structures. These breaker-height variations in-

144

duce alongshore gradients in set-up, which drive longshore currents and hence sediment transport. In our work, alongshore variability in breaker heights is related to wave refraction rather than to wave diffraction, but the subsequent mechanism for alongshore sediment transport remains the same.

To compute the sediment transport rate according to eq. 2, $H_b(y,t)$ and $\theta_b(y,t)$ are needed. The procedure to determine them is as follows. It is assumed that the wave height and wave angle are alongshore uniform in deep water. Then, wave transformation, including refraction and shoaling, is performed from deep water up to the breaking point so that $H_b(y,t)$ and $\theta_b(y,t)$ are determined and Q can be computed. To do the wave transformation, a perturbed nearshore bathymetry coupled to the shoreline changes is assumed:

$$D(x, y, t) = D_0(x) - \beta f(x) x_s(y, t)$$
(3)

where D(x, y, t) and $D_0(x)$ are the perturbed and unperturbed water depth, respectively, and f(x) is a shape function. Figure 2a shows some examples of possible perturbation profiles: constant bed perturbation in the surf zone and decreasing exponentially in the offshore direction (P1), bed perturbation decreasing exponentially in the offshore direction from the coast (P2), and bed perturbation similar to a shoal (P3 and P4).

The offshore extension of the bathymetric perturbation is controlled by its "characteristic" length, xl, which is a free parameter in the model. It was shown by $Falqu\acute{e}s$ and Calvete [2005] that the coupling between the surf and shoaling zones is crucial for
HAWI. This is accomplished only if xl is at least a couple of times larger than the surf
zone width. The parameter xl can be seen as a way to parameterise cross-shore sediment
transport, especially between the surf and shoaling zones. This makes HAWI essentially

different from the surf zone morphodynamic instabilities that lead to rhythmic bars and rip channels. The changes in the shoreline cause changes in the bathymetry (both in the surf and shoaling zones), which in turn cause changes in the wave field. The changes in the wave field affect the sediment transport that drives shoreline evolution. Therefore, the shoreline, the bathymetry and the wave field are fully coupled.

Following the linear stability concept, the perturbation of the shoreline is assumed to
be

$$x_s(y,t) = ae^{\sigma t + iKy} + c.c. (4)$$

where a is a small amplitude. For each given (real) wavenumber, K, this expression is inserted into the governing equation (eq. 1), and into the perturbed bathymetry equation (eq. 3). By computing the perturbed wave field and inserting H_b and θ_b in eq. 1, the complex growth rate, $\sigma(K) = \sigma_r + i\sigma_i$, is determined. All of the equations are linearized with respect to the amplitude, a. Then, for those K such that $\sigma_r(K) > 0$ a sandwave with wavelength $\lambda = 2\pi/K$ tends to emerge from a positive feedback between the morphology and the wave field. The pattern that has the maximum growth rate is called the Linearly Most Amplified mode (LMA mode).

3. Numerical experiments on idealised cases

To investigate the possible mechanism causing shoreline instabilities under low wave incidence angles, numerical experiments on idealised cases are performed. First, numerical experiments and results are given. Then, a sensitivity study is done to assess better the results.

3.1. Instabilities versus beach slope and wave incidence angle

3.1.1. Configuration

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A Dean profile (Figure 2b) is chosen as the equilibrium profile, using various beach slopes (Figures 2b and c). The adopted profile is given by:

$$D_0(x) = b\left((x+x_0)^{2/3} - x_0^{2/3}\right)$$
 (5)

which has been modified from the original Dean profile to avoid an infinite slope at the 210 shoreline. The constants b and x_0 are determined from the prescribed slope β at the 211 coastline and the prescribed distance x_c from the coastline to the location of the closure depth D_c (see Falqués and Calvete [2005] for details). The forcing conditions are waves 213 with $H_{rms} = 1.5$ m and Tp = 8 s at a water depth of 25 m. The wave direction ranges from 0° to 85° in increments of 5° . A closure depth $\bar{D}=20$ m is chosen. To perform the 215 linear stability analysis, the shape function for the bathymetric perturbations is assumed 216 to be constant in the surf zone and to decrease exponentially seaward. Its cross-shore 217 extent is given by the characteristic distance xl corresponding to the closure depth of 20 218 m, i.e. xl = 1410 m for the present case (P1-perturbation in Figure 2a). 219

220 **3.1.2.** Results

Figure 3a shows the growth rate of the LMA mode versus the wave angle and the beach slope. The wave angle is given for a water depth of 25 m. The beach slope is defined as the beach slope at the shoreline. For small beach slopes (< 0.04) the coast behaves as expected: it is unstable only if the wave incidence angle is large enough. In this case, the shoreline instabilities clearly correspond to HAWI. For instance, for a beach slope of 0.02,

a wave incidence of 70° leads to the largest growth rate $(3.13 \times 10^{-9} \text{ s}^{-1})$, corresponding to a wavelength of 7000 m (Figure 3b).

However, for larger beach slopes, instabilities occur for all wave directions, and especially for low wave incidence angles. These instabilities correspond to what will be called LAWI in the present paper. Furthermore, among all the wave incidence angles, the most amplified mode is for shore-normal wave incidence. For a beach slope of 0.1, an angle of 0° leads to the largest growth rate $(1.82 \times 10^{-6} \text{ s}^{-1})$, corresponding to a wavelength of 571 m (Figure 3b).

3.2. Sensitivity analysis

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The sensitivity analysis is performed using a planar beach, as the aim is to focus on the mechanisms. However, simulations with other (e.g. barred) profiles also lead to LAWI (not shown).

3.2.1. Wave height and beach slope

Keeping the same reference configuration as above and focusing on shore-normal wave incidence, we investigate the sensitivity of the instability to the wave height for a range of beach slopes. For normally incident waves, instabilities develop only for a beach slope that exceeds 0.04 (Figure 4). In this case, there is an optimum in the wave height for which the growth rate is largest. This wave height increases with the beach slope. For instance, for a beach slope of 0.1 and 0.18), the optimal wave height H_{rms} is 1.75 m and 2.5 m, respectively. A wave height increase also leads to an increase in the LMA mode wavelength, which is due to the corresponding increase in surf zone width.

3.2.2. Bathymetric perturbation length

The influence of the parameter xl was previously investigated by $Falqu\'{e}s$ and Calvete [2005], who showed that xl must exceed a threshold to initiate HAWI (the perturbation must extend across both the surf and shoaling zones). Similar behaviour is found here by exploring the range between xl = 10 and $xl = 10^4$ m. Figure 5 shows that there is a

Figure 5

threshold, xl > 100 m, above which shoreline instabilities may occur. This value appears 251 physically reasonable since the width of the surf zone in the reference case is about 73 252 m. For $125 \le xl \le 250$ m, the shoreline instability wavelength decreases significantly (from 1040 to 530 m) with increasing perturbation length, whereas for $xl \geq 250$ m, the 254 wavelength increases only slightly until reaching a nearly constant value of 574 m. The growth rate increases with increasing xl for values below 500 m but decreases for xl256 exceeding 500 m, reaching a nearly constant value for large perturbation length scales. 257 The main conclusion is that instabilities occur only if the perturbation extends far enough 258 into the shoaling zone. When the perturbation length is about the width of the surf zone, 259 it influences the wavelength and growth rate of the LMA mode strongly, whereas for larger perturbation length values, this influence is negligible. 261

3.2.3. Initial perturbation shape

To evaluate the influence of the bathymetric perturbation shape function on the results
we have presented so far, several shapes were investigated using the same wave-boundary
conditions and a perturbation length xl of 2000 m. The shape functions we consider are
(Figure 2a):

• Perturbation P1: bed perturbation constant in the surf zone and decreasing exponentially in the offshore direction

- Perturbation P2: bed perturbation decreasing exponentially from the coast in the offshore direction
- Perturbation P3: P2 perturbation with a shoal located only in the shoaling zone, from 400 to 800 m, with a maximum height at $x_1 = 600$ m.
- Perturbation P4: P2 perturbation with a shoal located in both the surf and shoaling zones, from 0 to 1400 m, with a maximum height at $x_1 = 600$ m.

The reference configuration is still the same ($H_{rms}=1.5 \text{ m}$, T=8 s, $\theta=0^{\circ}$). The four shape functions result in LMA mode wavelengths of 571, 571, 608 and 608 m, respectively, and growth rates of 1.7, 1.5, 1.7, 1.7 $\times 10^{-6} \text{ s}^{-1}$, respectively. Thus, the results are slightly sensitive (mean wavelength of 598 m and a standard deviation of 18 m) to the bed perturbation type, but all perturbation types cause LAWI with similar growth rates.

3.2.4. Sediment transport equation

To investigate the sensitivity of the results to the sediment transport equation, compu-281 tations were carried out with r=0, which reduces eq. 2 to the CERC equation. This 282 sensitivity study is done in beach slope - wave angle space. The LMA characteristics are 283 quite similar with r=1 (Figure 3) and r=0 (Figure 6), except for the case of normal 284 wave incidence. In this case (r=0), for small beach slopes, all of the perturbations are damped, as for r=1. For larger beach slopes, the growth rate increases with decreasing 286 perturbation wavelength without reaching a local maximum (Figure 7). Thus there is no LMA mode for shore-normal wave incidence (X symbol on Figure 6). This specific case for 288 shore-normal wave incidence will be discussed in section 4. To summarize, the previous 289 results are not highly sensitive to the second term of the sediment transport equation, 290 except for the case of shore-normal wave incidence. 291

Figure 6

4. The physical mechanism

Here we investigate the physics behind the model prediction of shoreline instabilities
caused by low wave incidence angles. The physical processes are analysed based on the
study of the growth rate components, and the hydrodynamic and sediment transport
patterns, before identifying the main mechanisms.

4.1. Growth rate analysis

In the perturbed situation where the shoreline position is given by eq. 4, the wave height and wave angle at breaking are given by:

$$H_b(y,t) = H_b^0 + (\hat{H}'_{br} + i\hat{H}'_{bi})e^{\sigma t + iKy} + c.c.$$

$$\theta_b(y,t) = \theta_b^0 + (\hat{\theta}'_{br} + i\hat{\theta}'_{bi})e^{\sigma t + iKy} + c.c.$$
(6)

where H_b^0 , θ_b^0 are the wave height and angle for the unperturbed situation. Then, according
to Falqués and Calvete [2005], the growth rate (the real part of the complex growth rate)
is:

$$\sigma_r = \underbrace{2\frac{\mu}{\overline{D}}H_b^0 K^2 \cos\left(2\theta_b^0\right)}_{e_0} \left(\underbrace{-1}_{e_1} + \underbrace{\frac{\hat{\theta}'_{bi}}{aK}}_{e_2} + \underbrace{\frac{5\hat{H}'_{bi}}{4aKH_b^0} \tan\left(2\theta_b^0\right)}_{e_3} - r\frac{\hat{H}'_{br}}{a\beta} \frac{\cos\left(\theta_b^0\right)}{\cos\left(2\theta_b^0\right)}\right)$$
(7)

A clue to the physical mechanism is provided by a careful analysis of the meaning and behaviour of each term:

- e_0 : common to all terms. It does not contribute to the stability/instability since it is positive. This is because we can assume that $\theta_b^0 < 45^{\circ}$ due to wave refraction. It is the magnitude of the growth rate.
- e_1 : always negative. It represents the contribution due to the changes in shoreline orientation when there is no perturbation in the wave field. This is the only term arising

in case of the classical analytical one-line modeling (Pelnard-Considère equation) [Dean and Dalrymple, 2002]. It is a damping term describing the shoreline diffusivity in that approach.

• e_2 : its sign depends on $\hat{\theta}'_{bi}$. Numerical computations [Falqués and Calvete, 2005]
demonstrates that it is always positive. This results from the fact that refracted wave
rays tend to rotate in the same direction as the shoreline. Thus e_2 is a growing term.

• e_3 : its sign depends on \hat{H}'_{bi} . Numerical computations [Falqués and Calvete, 2005] show that $\hat{H}'_{bi} > 0$ for long sandwaves and < 0 for short sandwaves. This term is related to energy spreading due to wave crest stretching as waves refract. Thus e_3 is a growing or damping term, depending on the sandwave wavelength, $2\pi/K$. Moreover, its magnitude increases with an increasing incident wave angle. These two properties explain that e_3 is an essential growing term for HAWI formation Falqués and Calvete [2005], whereas, for LAWI, its magnitude is smaller and it is, most of the time, negative.

• e_4 : this term stems from the alongshore gradients in H_b in the sediment transport equation (eq. 2). Its sign is the opposite to that of \hat{H}'_{br} , which is numerically found to be always positive. This is related to the fact that the maximum in wave energy is always located close to the sandwave crest (wave focusing). Thus e_4 is a damping term.

The corresponding growth rate contributions, $\sigma_1 = e_0 e_1$, $\sigma_2 = e_0 e_2$, ... are plotted in Figure 8. It can be seen that σ_2 is always positive leading to the development of shoreline sandwaves, whereas σ_1 and σ_4 are always negative, leading to the damping of the sandwaves. The term σ_3 can be either positive, for small beach slope (eg smaller than 0.05 to 0.08), or negative, for larger beach slopes. Even if the behaviour of this term is not monotonous, σ_3 generally increases with the wave angle. It is remarkable that σ_2 becomes

very large for large beach slopes and for small wave angles. For normal wave incidence $(\theta_b^0 = 0)$, $\sigma_3 = 0$ and σ_2 is the only contribution leading to the instability. We therefore conclude that wave refraction is responsible for LAWI in the case of very steep beach slopes.

Based on the growth rate results, it is also possible to analyse the relative influence 335 of the wave incidence induced Q_1 and wave set-up induced Q_2 sediment transport. The 336 analysis of the growth rate versus the perturbation wavelength for r=0 or r=1 and 337 several wave incidence angles θ (Figure 9) shows that the relative influence of Q_2 decreases 338 with increasing the wave incidence angle. In other words, wave height gradients (wave setup induced sediment fluxes) largely influence (damp) the shoreline instability for low wave 340 angle incidence (LAWI), whereas their impact is almost negligible for large wave incidence 341 angles (HAWI). The main driving term of the LAWI is due to the wave incidence induced 342 sediment transport flux Q_1 . This means that the use of the CERC equation alone, taking 343 into account wave refraction in the shoaling zone, can cause LAWI. The Q_2 term influences this instability by changing the growth rate and the favored wavelength. This influence 345 increases with decreasing wave incidence until the case of perfectly shore-normal waves, for which there is a preferred wavelength (LMA mode) only if the Q_2 term is taken into 347 account (Figure 6).

4.2. Model results analysis: Hydrodynamic and sediment transport

To understand better how wave refraction causes shoreline instabilities, hydrodynamic and sediment transport model results are analysed next. Here, we focus on the case of shore-normal wave incidence, considering the LMA mode obtained for a beach slope equal to 0.1 (case a). The model results are compared with the same wave incidence, but

a smaller beach slope (0.02) for which the shoreline is stable (case b). The perturbation 353 wavelength (571 m) is the same for both cases, corresponding to the LMA mode of case (a). Although the linear stability analysis is strictly valid only in the limit $a \to 0$ we 355 choose a shoreline sandwave amplitude a = 10 m (for visualization and comparison of 356 the different sources of sediment transport). In addition, to make the analysis simpler, 357 we assume shore-normal waves and r=0. Figures 10a and b show planviews of the 358 wave angle, as well as a longshore cross-section of several quantities along the breaking 359 line. First, it can be noted that the breaking line is much farther offshore in case (b) 360 because of the shallower bathymetry. This is directly linked with the bathymetry. These planviews illustrate the wave focusing on the cusp, which implies increasing wave height 362

and converging waves at the cusps.

Looking at the alongshore cross-section (Figure 10c), the wave angle amplitude is much 364 larger for case (a) than for case (b), about 14° versus 3.2°, indicating a stronger refraction 365 up to the breaking line in case (a). The corresponding amplitude of the oscillation in the shoreline angle is about 6.3°, and is thus within the range of those two values. This 367 means that the angle of the wave fronts with respect to the local shoreline reverses when passing from case (a) to (b), implying a reversal in the direction of sediment transport. 369 This can be traced back to equation 6. The wave angle amplitude is much larger for case 370 (a). Coming back to equation 6, in the case of shore-normal waves and r=0, there are 371 only two terms left: e_1 , which is the contribution due to shoreline change only, and e_2 , 372 which represents the wave refraction-induced sediment flux. The analytical computation 373 for the present case leads to: $e_1 = -1$ for both cases, whereas $e_2 = 2.23$ for case (a) and 374 $e_2 = 0.507$ (case b), consistent with the different amplitudes of alongshore wave angle

oscillation. This clearly shows that the growth rate is positive for case (a) and negative 376 for case (b). The alongshore cross-section of the resulting sediment flux Q (Figure 10c) illustrates the opposite behaviour for the two cases. Our sign convention is that positive 378 Q represents sediment transport directed in the direction of the increasing y coordinate 379 (i.e. to the right on the cross-sections). A positive (negative) longshore gradient indicates 380 a convergence (divergence), assumed to cause shoreline accretion (erosion). Thus Figure 381 10c shows that Q for case (a) has a spatial phase-lag compared to the shoreline such that 382 the shoreline perturbation should be amplified, whereas Q for case (b) has an opposite 383 phase-lag, leading to the damping of the perturbation. This spatial phase-lag change results from the continuous amplitude changes of the terms e_1 and e_2 : the phase-lag 385 between shoreline and longshore sediment fluxes is either 90° or -90° , implying that 386 there is no migration and either amplification or damping of the shoreline perturbation. 387 Thus, for shore-normal waves and neglecting the damping term related with wave set-388 up induced sediment flux (second term in eq. 2), the instability of the shoreline results from an alongshore oscillation in the angle of wave refraction, which is stronger than the 390 oscillation in the angle of shoreline orientation.

4.3. Mechanism

From the above, we can draw the following conclusion: the main growing term is related to the wave refraction toward the cusp, leading to wave incidence induced sediment
transport converging at the cusp. This term strongly increases with beach slope. The
damping is due to three components: (1) longshore sediment transport due to the shoreline orientation only (and not refraction, term e_1), (2) wave energy spreading (term e_3),

damping effect than the two others.

Figure 11

Now we can figure out how LAWI works (Figure 11). Let us consider shore-normal 399 wave incidence. In this case, the wave energy spreading has no influence on the instability 400 $(e_3 = 0)$. If a cuspate feature with an associated shoal develops on a coastline, wave 401 refraction bends wave rays towards the tip of the feature. Depending on the orientation 402 of the refracted wave fronts with respect to the local shoreline along the cuspate feature, 403 the alongshore sediment flux can be directed towards the tip, reinforcing it and leading to 404 a positive feedback between flow and morphology. Whether the transport is directed to the tip, depends on the bathymetry and wave conditions. For a given offshore extent, xl, 406 of the associated shoal and a given wave height, the surf zone will become narrower if the 407 beach slope increases. Then, the shoal will extend a longer distance beyond the surf zone, 408 and the waves will be refracted strongly when they reach the breaking point, increasing 409 the wave incidence related sediment flux (e_2) convergence whereas the divergence term 410 (e_1) is constant. As shown by the model results (Figure 10), the contribution of the 411 refracted wave angle (e_2) can exceed the contribution of the shoreline orientation to the 412 sediment flux (e1), such that Q_1 (resulting from e_1 and e_2) converges near the cusp. This 413 leads to the development of the cusp. If the beach slope is mild, the surf zone will be 414 wider, and wave refraction over the shoal before breaking will be less intense, leading to 415 smaller wave incidence angle induced sediment fluxes, which are dominated instead by the 416 diverging sediment flux induced by shoreline orientation changes. In this case, as shown in the model results (Figure 10c), the sediment flux is directed away from the tip of the 418 cusp.

5. Discussion

5.1. Linear stability analysis validity

The 1D-morfo model has been applied to investigate HAWI and to study the sandwaves 420 generation along the Dutch coast [Falqués, 2006], El Puntal beach - Spain [Medellín et al., 421 2008, 2009. The results indicated similarities with the wavelengths observed in nature. 422 This supports the use of this linear stability model to investigate the mechanisms of shore-423 line sandwave formation. In the present paper, it is clear that LAWI is a robust output 424 of the 1D-morfo model, and the physical mechanism causing instabilities is wave refrac-425 tion induced by an offshore shoal associated with a cuspate feature. This wave refraction leads to two counter-acting phenomena: sediment transport induced by converging waves 427 counteracted by diverging wave height gradients. The present paper investigates the linear generation only. The pros and cons of linear stability analysis have been discussed 429 extensively in [Blondeaux, 2001; Dodd et al., 2003; Falqués et al., 2008; Tiessen et al., 430 2010. In any case, the fundamental assumption of infinitesimal amplitude growth makes 431 comparisons to field data questionable. Nonlinear model studies for other rhythmic fea-432 tures, such as crescentic sandbars and sand ridges [Calvete, 1999; Damqaard et al., 2002], 433 have sometimes shown the finite-amplitude dynamics to be dominated by the LMA mode 434 in other cases, modes other than the LMA became dominant. We leave the nonlinear modeling of LAWI, including the study on cessation of the growth, to future work. 436

5.2. Analogy with megacusps: growth rates and circulation patterns

Although the model results are given for a planar beach, LAWI is also found in the presence of a shore-parallel bar (not shown). Thus, for intermediate morphological beach state where crescentic bars and associated megacusp systems usually develop, the model rate comparable to that of co-existing instabilities. Our sensitivity studies indicate LAWI growth rates to range from 10⁻⁶s⁻¹ (for a beach slope of 0.05) to 10⁻⁵s⁻¹ (for a beach slope of 0.2). The typical generation time scale thus ranges from 1.5 to 11.5 days. These time scales were obtained for shore-normal waves having a moderate wave height of 1.5 m and wave period of 8 s. A typical time scale for the LMA mode of crescentic bars is several days [Damgaard et al., 2002; Garnier et al., 2010]. Thus, for specific beach slope and wave conditions, the LMA shoreline instabilities have comparable initial growth rates as those of crescentic bar patterns.

Computations for the idealized cases gives LAWI wavelengths of the same order of
magnitude as the observed spacing of crescentic bars and associated megacusps. The
distinction between these two kinds of instabilities is therefore difficult and the validation
of the presence of LAWI in a Rhythmic Bar and Beach morphological environment is not
straightforward. More generally, a proper validation of the present results would need
dataset of shoreline evolution, together with bathymetric, wave and current data, starting
from an initial longshore uniform beach. To our knowledge, such data do not exist.

Although we cannot validate the model results with wavelengths observed in the field,
it is possible to discuss whether the type of nearshore circulation linked to LAWI, that is,
a longshore sediment flux pointing toward the cuspate feature at both sides, is realistic or
not in nature and in the framework of 2DH modeling. According to *Komar* [1998], both
types of longshore current patterns, either converging or diverging at a megacusp, are
observed in nature. Another example showing that this type of circulation is realistic is
the case of a submerged breakwater. Both observations and numerical modelling indicate

that if the breakwater is beyond the breaker line, the waves drive longshore currents that 463 converge at the lee of the breakwater to build a salient [Ranasinghe et al., 2006]. This converging type of circulation at a megacusp was also observed by Haller et al. [2002] in 465 laboratory experiments on barred beaches with rip channels. One of their six experimental 466 configurations may be quite close to a LAWI configuration. This configuration had the 467 largest average water depth at the bar crest and the smallest rip velocity at the rip neck, 468 such that, in addition to the rip current circulation, they found a secondary circulation system near the shoreline, likely forced by the breaking of the larger waves that propagated 470 through the channel. As these waves are breaking close to the shoreline, they drove longshore currents away from the rip channels into the shallowest area. This experiment 472 shows that breaking close to the shoreline counteracts the rip-induced circulation, leading 473 to current convergence in the shallowest area. 474

The studies of Calvete et al. [2005] and Orzech et al. [2011] give other elements to 475 investigate the plausibility of the LAWI mechanism, in rip channels configurations. For 476 the case of a barred-beach, Calvete et al. [2005] developed a 2DH linear stability model, 477 having a fixed shoreline, that describes the formation of rip channels from an initially straight shore-parallel bar. For shore-normal waves, the circulation linked to rip channel 479 formation is offshore through the channels and onshore over the shoals or horns of the developing crescentic bar as is clearly observed in nature (e.g. [MacMahan et al., 2006]). 481 However, they also noticed small secondary circulation cells near the shoreline flowing in 482 the opposite direction, leading to presence of megacusp formed in front of the horns of 483 the crescentic bar; therefore, the shoreline undulations were out of phase (spatial phase-484 lag of 180°) with the crescentic bars, meaning that the amplitude of the wave-refracted

terms should dominate the amplitude of the wave set-up terms (Eq. 2). The formation of 486 those megacusps was not part of the instability leading to the crescentic bar development but was forced by the hydrodynamics associated with it. More importantly, the small 488 secondary circulation cells were essentially related to wave refraction: if wave refraction 489 from the model was eliminated, they did not develop. Thus, wave refraction by offshore 490 shoals (those of the crescentic bar in this case) can induce a circulation that may move 491 sediment toward a developing cuspate feature. A recent study, based on both observation 492 (video images) and non-linear morphodynamic modeling [Orzech et al., 2011] also showed 493 the occurrence of two types of megacusp (shoreward of the shoal or shoreward of the rip), and the associated converging sediment fluxes toward the megacusps. This tends to 495 support our mechanism analysis of LAWI formation. 496

The similarity between LAWI and megacusps in both wavelength and growth time 497 is certainly intriguing given the fact that 1D-morfo is mainly based on the gradients 498 in longshore sediment transport and wave set-up induced sediment transport (damping 499 term), but neglects many surf zone processes like rip current circulation, which is known 500 to be essential to crescentic bar dynamics [Calvete et al., 2005; Garnier et al., 2008]. However, the analysis above tends to show that there could be configurations, where the 502 processes taken into account in 1D-morfo are dominant in the system, at the initial stage. 503 This could explain why similarities are observed with the various numerical experiments 504 done with more sophisticated models. Furthermore, we should keep in mind the fact that 505 the LAWI mechanism is not related to any longshore bar, and thus that short shoreline sandwayes such as megacusps could develop without a bar, whereas it was thought that, 507 for barred beaches, short shoreline sandwayes develop due to surf zone sand bar variability.

6. Conclusions

A one-line linear stability model, which was initially created to describe the formation of shoreline sandwaves under high-angle wave incidence, has revealed shoreline instabilities for low to shore-normal wave incidence (LAWI). The most amplified mode has wavelengths of ~ 500 m and characteristic growth time scales of a few days, which are smaller than those of the high angle wave instabilities. Sensitivity analyses focusing on wave height, wave incidence angle, beach slope, beach profile, model free parameters and the sediment transport equation show that, for low to shore-normal wave incidence, instabilities develop for sufficiently large beach slopes (e.g. 0.06) and for sufficiently small wave heights (smaller than 2 m for a beach slope of 0.06).

The main process causing the instabilities for low to shore-normal wave incidence is wave refraction on a shoal in the shoaling zone, which focuses wave fronts onshore of it, leading to wave incidence induced sediment transport converging at the cusp. This effect strongly increases with beach slope. The damping is due to three longshore transport components:

(1) that caused by shoreline orientation only (and not refraction), (2) that caused by wave energy spreading (minor effect for low-angle wave incidence), (3) that caused by wave height gradients (set-up). Whether LAWI develops or not depends on the balance between these growing and damping terms. If this shoreline sand accumulation can feed the initial shoal through cross-shore sediment transport, a positive feedback arises.

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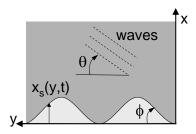


Figure 1. Sketch of the geometry and the variables. The angle between the wave fronts and the local shoreline is $\alpha = \theta - \phi$.

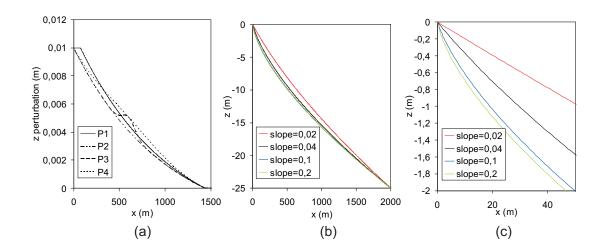


Figure 2. Bathymetric perturbations (a) and cross-shore Dean beach profile for a various beach slopes (b,c). P1-perturbation: constant in the surf zone and exponential decrease, P2-perturbation: exponential decrease, P3-perturbation: exponential decrease with a shoal in the shoaling zone, P4-perturbation: exponential decrease with a shoal in the surf and shoaling zones.

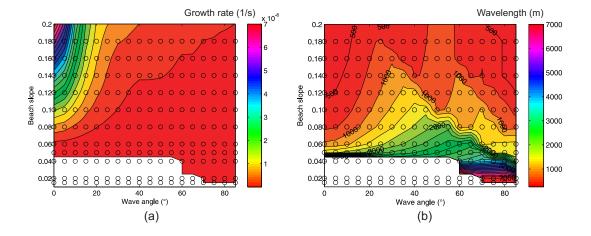


Figure 3. LMA (a) growth rate and (b) wavelength as a function of beach slope and angle of incidence. Circles indicate the 1D-morfo computations. In white: no growing perturbation. The model parameters are: $\mu = 0.15$, r = 1, P1-Perturbation and xl=1410 m for Dean profiles with $H_{rms} = 1.5$ m and $T_p = 8$ s at a water depth of 25 m.

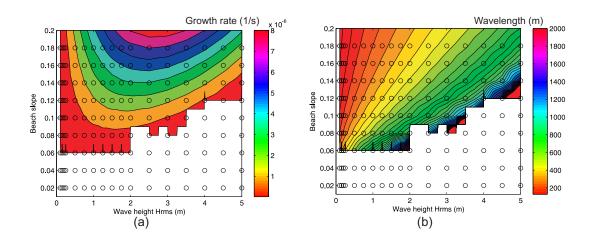


Figure 4. LMA (a) growth rate and (b) wavelength as a function of beach slope and wave height, for shore-normal waves. Circles indicate the 1D-morfo computations. In white: no growing perturbation. The model parameters are : $\mu = 0.15$, r = 1, P1-Perturbation and xl=1410 m for Dean profiles with $\theta = 0^{\circ}$ and $T_p = 8$ s at a water depth of 25 m.

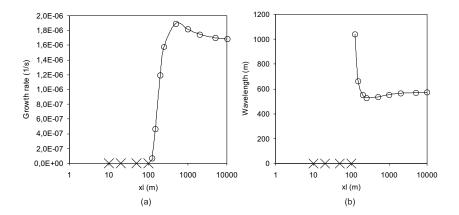


Figure 5. LMA mode (a) growth rate and (b) wavelength as a function of the shoreline perturbation length xl for a Dean profile with a beach slope of 0.1. Crosses on the xl axis $(10 \le xl \le 100)$ indicate that there is no LMA mode for the given shoreline perturbation length.

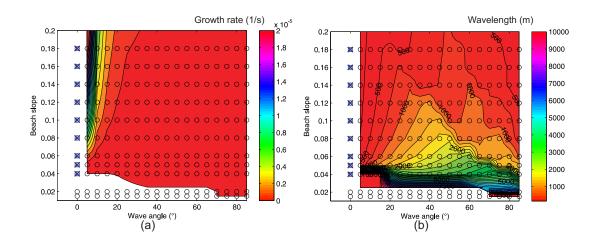


Figure 6. LMA (a) growth rate and (b) wavelength as function of beach slope and wave angle, for r = 0. Circles indicate the 1D-morfo computations. In white: no LMA mode. The symbol x indicates that, even if the growth rate was positive, there was a singularity at $\theta = 0^{\circ}$ (growth rate continuously increasing with decreasing wavelength), and therefore no LMA mode (see Figure 7).

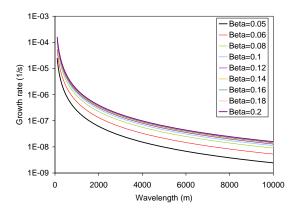


Figure 7. LMA growth rate versus wavelength for various beach slopes, using r=0 and shore-normal waves. The shoreline is stable for a beach slope $\beta < 0.05$. The model parameters are : $\mu = 0.15$, P1-Perturbation and xl=1410 m for the Dean profile with $H_{rms} = 1.5$ m and $T_p = 8$ s at a water depth of 25 m.

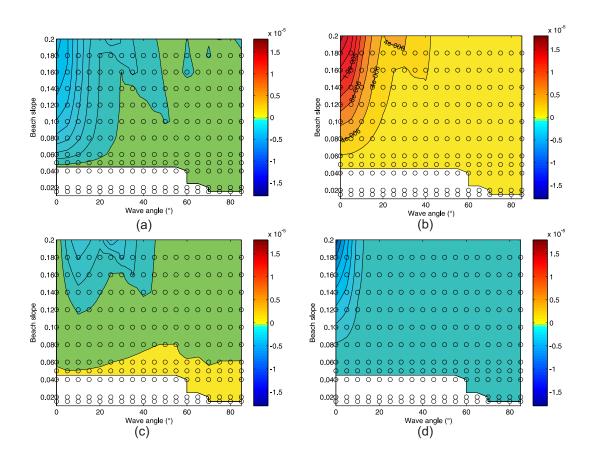


Figure 8. Growth rate components for the LMA mode as a function of beach slope and angle of incidence. Model paremeters are: $H_{rms} = 1.5 \text{ m}$, $T_p = 8 \text{ s}$ and cross-shore perturbation of type P1 with xl = 1410 m. (a) σ_1 , (b) σ_2 , (c) σ_3 , (d) σ_4 . Circles indicate the 1D-morfo computations. In white: no LMA mode.

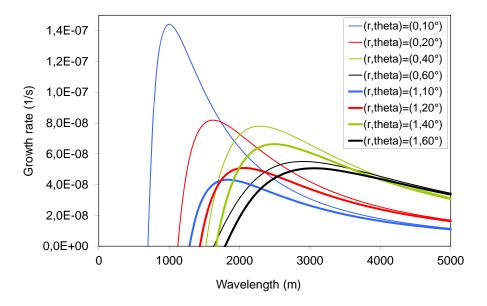


Figure 9. Growth rate versus wavelength for several combinations of r and wave incidence angle θ . The beach slope is 0.05.

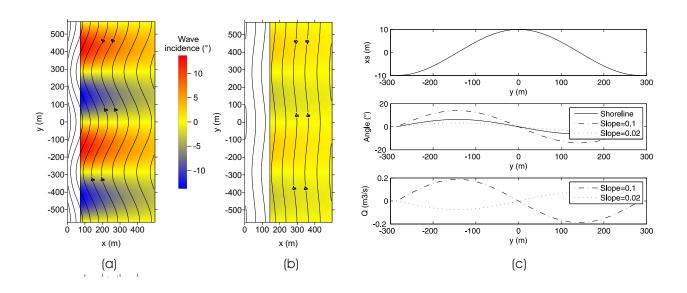


Figure 10. Model results for a perturbation wavelength of 571 m (LMA mode for a beach slope of 0.1), shore-normal wave incidence, and a shoreline wave amplitude of a = 10 m. (a) and (b) show the topographic contours and the refracted wave angle for beach slopes of 0.1 (a) and 0.02 (b). (c) shows the longshore profiles of (Top) the shoreline position, (Middle) the shoreline angle (solid line) and refracted wave angles and (Bottom) the sediment fluxes. Dashed-dotted lines, and dotted lines represent a beach slope of 0.1 and 0.02, respectively.

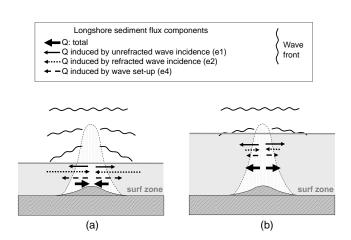


Figure 11. Sketch of the physical mechanisms causing LAWI. Sediment transport components induced by a shoal for unstable (a) and stable (b) situations, corresponding to a narrow and wide surf zone, respectively.